

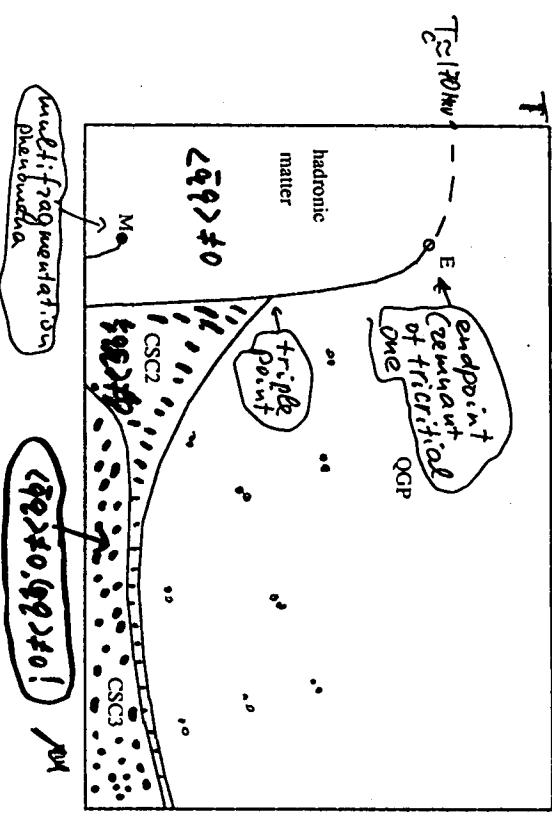
QCD in the extreme conditions

E.V.Shuryak, Stony Brook

Before we start, we need some maps...
The theoretical version

Lecture 1: The phases of QCD

- Prolog: Current phase diagram as a map
- Chiral symmetry breaking in vacuum and instantons
- What happens at non-zero T: lattice, instanton molecules
- Properties of Quark-Gluon Plasma
- Color Superconductivity at high density
- Color Superconductivity at very high density
- Other “extreme conditions”: increasing number of quark flavors, adjoint fermions, SUSY theories...



- Progress was most significant in the large density low T region. New phases: 2-flavor-like and 3-flavor-like Color Superconductors. (see talks by K.Rajagopal and T.Schaefer). Unfortunately the paths for heavy ion collisions do not cross them.
- Another new element: the (remnant of) the QCD tricritical point (see talks by K.Rajagopal and M.Stephanov). Strongly depends on m_S ...

- “TRIALITY”

(1)

(2)

Instantons in QCD vacuum

$$\frac{d\epsilon}{d\bar{q}} \quad A_\mu = \frac{2}{3} \frac{\eta_{\mu\nu}^a X^a}{\bar{q}^3}$$

describes
fumelling between
topologically different
vacua...

[Gell-Mann et al (1976)]

(although different)

otherical Nambu-Jona-Lasinio
tion, which is to create
 $\langle \bar{q} q \rangle \neq 0$ pions and all that

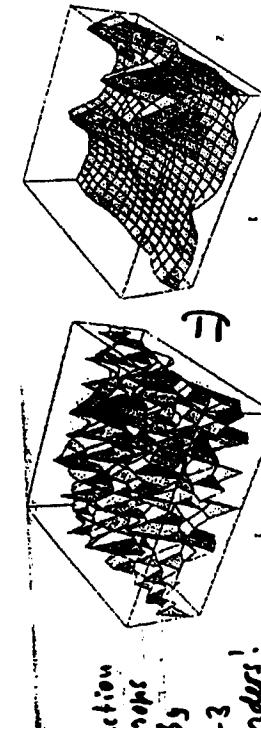
also $\eta' \rightarrow$ (sign opposite!)

12) \rightarrow Instantons create $\bar{q} q$, etc !

$n \cdot n + n \approx 1 \text{ fm}^{-4}$, $g \approx \frac{1}{3} \text{ fm}$
mass parameter $n g^4 \sim (\frac{1}{3})^4 \ll 1$!

3

nders!



Before \downarrow and \uparrow after (25 cooling)
the fog steps goes away ...

$$\boxed{\begin{array}{l} \text{Very close to} \\ \text{my } \xi = \eta_3, R \cdot 1/f_m \\ \hline \xi = 0.35 \text{ fm} : R \approx 0.9 \text{ fm} \end{array}}$$

+ many others

Chiral symmetry breaking and restoration

Few facts from the textbooks:

- If quark masses are ignored, the QCD Lagrangian is a sum of independent left and right-handed parts. This generates two chiral symmetries, having rather different fate:
- The $U(1)_A$ part is explicitly broken by anomaly, which (as G. t'Hooft and others explained) is driven by instantons. The measure of (rather significant!) strength of this effect is deviation of η' mass from that of a pion/kaon.

\rightarrow

works repulsively for η'
but it also works
attractively for π ...
 \rightarrow does not work for η, ω ...

- The $SU(N_f)$ part is spontaneously broken, leading to non-zero quark condensate $\langle \bar{q} q \rangle$, pions and all that. The reason for that is strong attraction between quark and antiquark in scalar channel, e.g. as assumed by Nambu-Jona-Lasinio (NJL) model (Nambu and Jona-Lasinio, 1961).

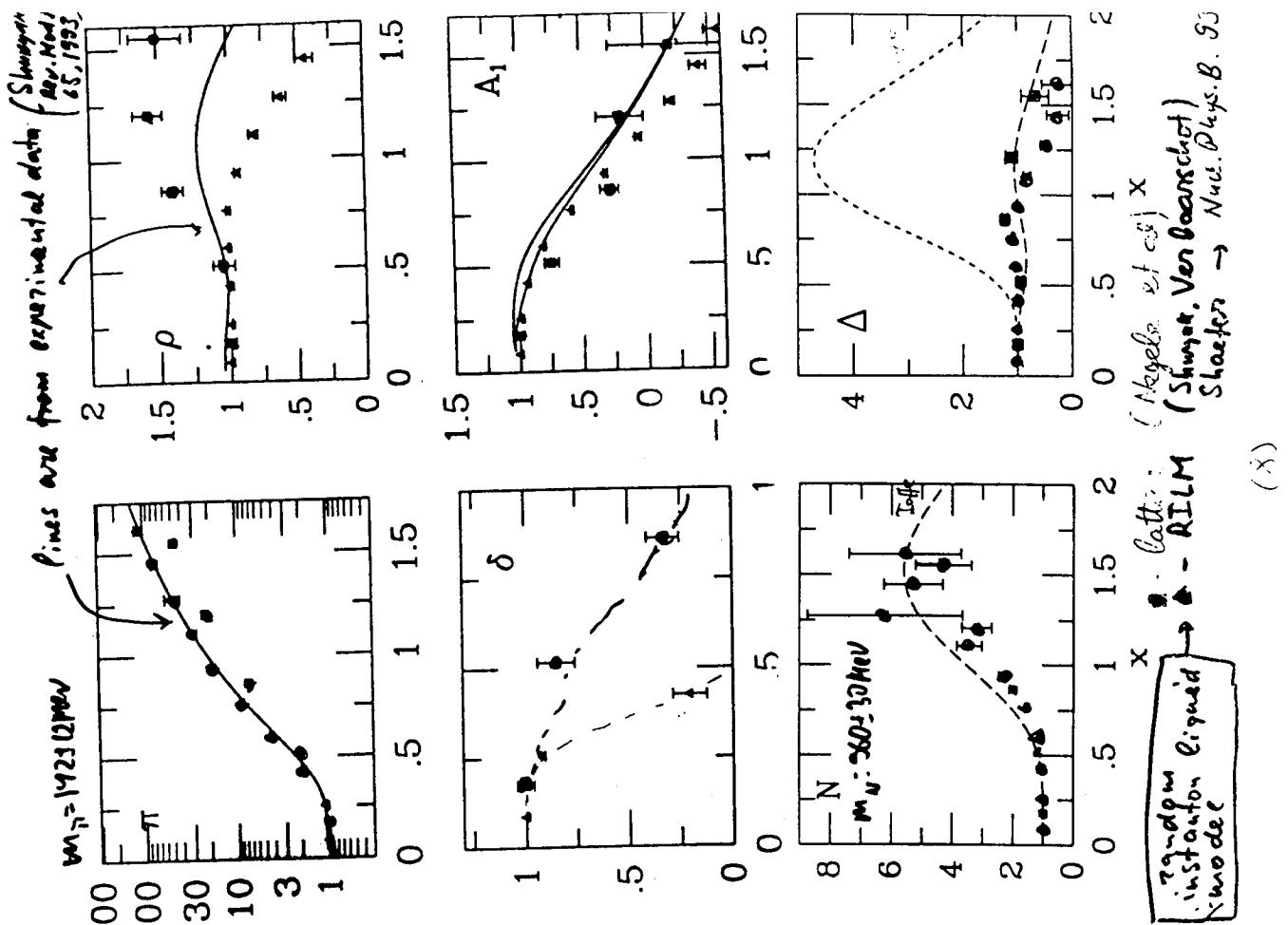
Interactions (III)

More recent findings(/claims) :

- - $SU(N_f)$ Chiral symmetry breaking is also caused by instantons. The same t'Hooft interaction which violates $U(1)_A$ is the attraction needed for it. However spontaneous breaking is not single-instanton effect, but a result of collective interaction of all instantons. (Therefore $\langle \bar{q}q \rangle \sim \sqrt{n_{\text{instantons}}}$, not the first power.) (E.Shuryak 1982, D.Diakonov and V.Petrov, 1986.)
- - Lattice works of 80's have found chiral restoration phase transitions in QCD, at rather low temperature $T_c \approx 150 \text{ MeV}$. Its order is still not clear, but it is sharp enough, transition to QGP happens in a narrow interval not larger than $\delta T \sim 10 \text{ MeV}$.
- - Studies of susceptibilities, correlation functions, "screening masses" etc have shown that in scalar and pseudoscalar channels like π, σ, η' significant changes occur, and deviations from free quark behavior persist to the $T > T_c$ phase. However no large deviations in vector and axial channels are so far found.

- - Instanton liquid model has reproduced (nearly) all those features of chiral restoration (Th.Schafer and Shuryak,96). In addition, it suggests a simple mechanism for chiral restoration: formation of instanton-anti-instanton molecules. Recently first direct observation of molecules were made on the lattice ((Ph. de Forcrand, 98))
- - Instantons were shown to generate Color Superconductivity at high density and relatively low $T < 50 \text{ MeV}$. (Rapp,Schafer,Shuryak,Velkovsky, PRL 98, Alford, Rajagopal, Wilszek PLB 98) Unfortunately lattice simulations are not yet possible for non-zero chemical potential to study this region.
- - Existence of the "endpoint" second order transition in which sigma is truly massless, and especially its possible observation in heavy ion collisions was discussed (Stephanov,Rajagopal,Shuryak 98)

$$\begin{matrix} y \\ f \\ (G) \end{matrix}$$



How to describe
the instanton-induced effects?

Way #1: First integrate away the color field A_μ^a

\Rightarrow 't Hooft effective interaction (like Nambu-Jona-Lasinio...)

implies: short distance behaviour of $\chi\bar{\chi}$ correlators

$$\langle \chi(x) \rangle = \langle \chi(x) \rangle_0 + \langle \chi(x) \rangle_1 \quad \Rightarrow \quad \langle \chi(x) \rangle_1 = \frac{1}{N_c} \int d^4y \langle \chi(y) \chi(x) \rangle_{\text{pert}} \quad (\text{pert not exist!})$$

implies: sum of loops for $\langle \chi(x) \rangle_1$ is good!
(Diakonov, Petrov 86)

... But, how to solve it to all orders?

Way #2: First do fermions, in 'atomic' approximation, then average over coll. variables

$$Z \sim \int d\Omega e^{-S_g[\phi(t), \psi]} \quad \begin{matrix} \uparrow \text{fermionic interaction} \\ \uparrow \text{fermionic interaction} \\ \uparrow \text{collective coordinates} \\ \downarrow \text{instanton} \end{matrix}$$

Legend:
 - RILM \rightarrow instanton liquid model
 X lattice \rightarrow (Neglects inst.)
 \times Slawig \rightarrow Nucl. Phys. B. S_J

(7)

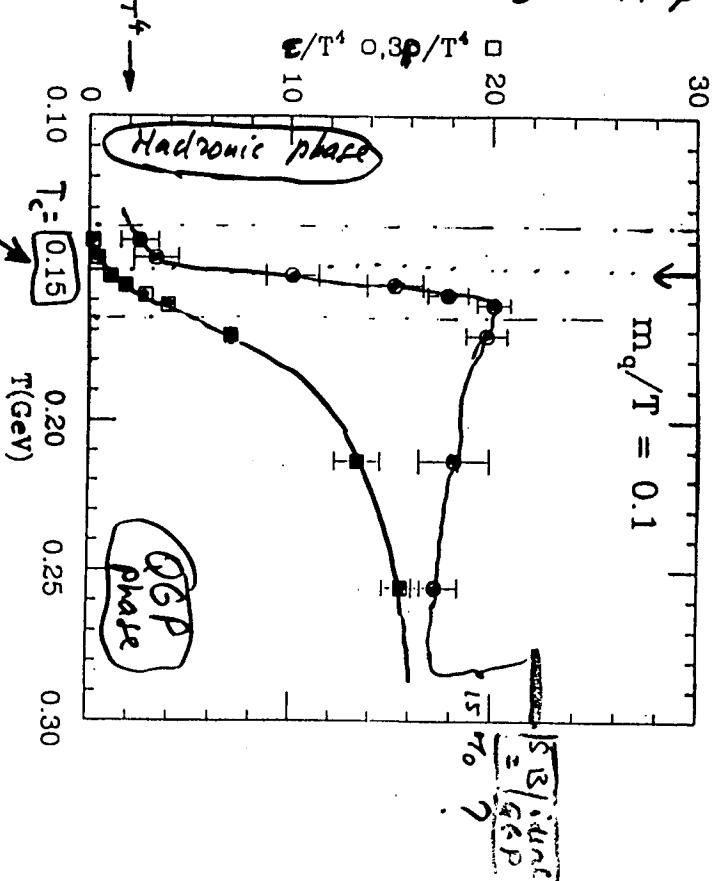
QCD Thermodynamics

On the Lattice

$$N_f = 2 \leftarrow \text{dynamical u, d}$$



energy density and pressure



Comment:

Pure glue \Rightarrow "deconfinement"

QCD with light quan.
"chiral restoration",

$$T_d \approx 260 \text{ MeV}$$

(Karsch et al) Both are surprisingly small ...

$$T_c \approx 150 \text{ MeV}$$

Why they are so different?

say tuned ...

- 1.
2. Energetics is very different
as can be seen from a QGP side
 $p_{\text{QGP}} = (\#) T^4 + \frac{B_{\text{QGP}}}{\text{small}} B^2$ should stay > 0
- * For pure glue ($T = T_d$) the first term is large and matches the vacuum energy $B_{\text{vac}}^2 / 4 \pi$ and $p_{\text{QGP}}(T = T_d + \varepsilon)$ is small but positive so $p_{\text{QGP}}(T = T_d + \varepsilon)$ is small but positive
- * For QCD ($T = T_c$) the first term is too small, all non-perturbative fields cannot dis-
- So, at $T \gtrsim T_c$: $B_{\text{QGP}} \approx \frac{1}{2} B_{\text{vac}}$!

(G.Brown, V.K.L.)

"Hard glue", or "epoxy" does not melt

What is it made of?

the vons
small
ship
is where all action is
= the mixed phase

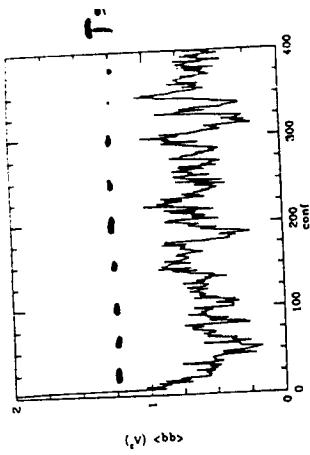
What is going on?

MILC - Collaboration
1994
T DeGrand et al.

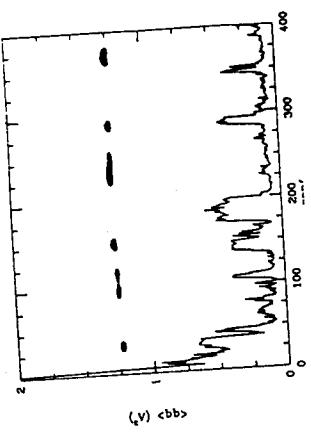
[QCD] \Rightarrow

Thermal Histories

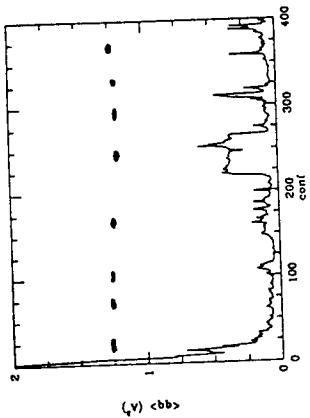
$T = 114 \text{ MeV}$



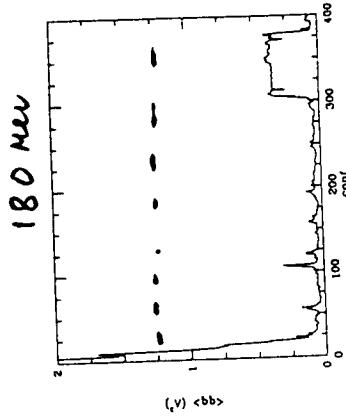
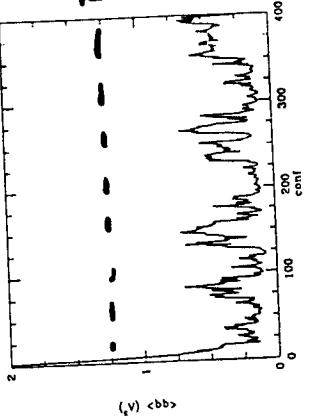
153 MeV



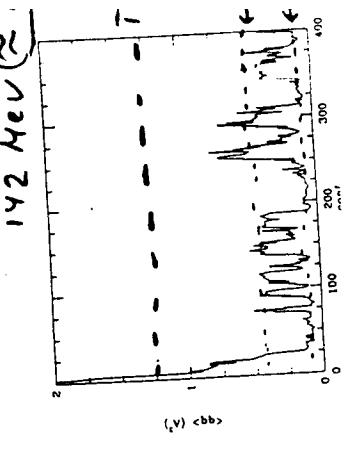
166 MeV



133 MeV



$142 \text{ MeV} (\approx)$

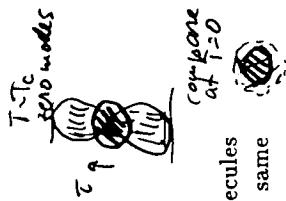


\Rightarrow weak 1-st order -

CHIRAL SYMMETRY RESTORATION

(based on T.Schaefter, E. Shuryak and J. Verbaarschot, The chiral phase transitions and the Instanton Molecules; SUNY-NTG-94-24, Stony Brook.)

- At growing T , quark motion becomes anisotropic Example: zero mode of the "caloron" ($T \neq 0$ instanton)



$$\psi(\tau, r) \sim |\sin(\pi T \tau) / \cosh(\pi T \tau)|^{2N_f}$$

oscillatory in time, exponentially decaying in space.

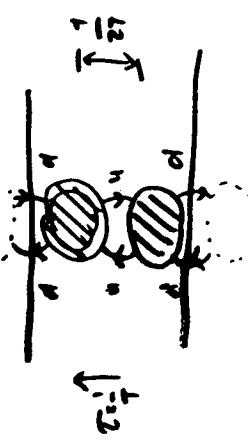
- A "pairing" of instantons (leading to formation of II molecules even at $T=0$) becomes much stronger, if I and II are at the same point

$$det D \sim |\sin(\pi T \tau) / \cosh(\pi T \tau)|^{2N_f}$$

Rapid "polarization" of even one molecule was found at $T \approx T_c$, which allows one to identify T_c as approximately the size of the "Matsubara box", such that exactly one molecule fits into it).

$$\Delta\tau = \frac{1}{2T} \text{ half box}$$

$$\Delta\tau = 0 \text{ same point}$$



↑ as maximum
↑ $T \approx 110 \text{ MeV}$
: 140 MeV it
makes!

↑ \approx size of a molecule!
↑ not true for smaller N_f ...

→ For $N_f = 2 \text{ to } 3$
(not true for smaller N_f ...)

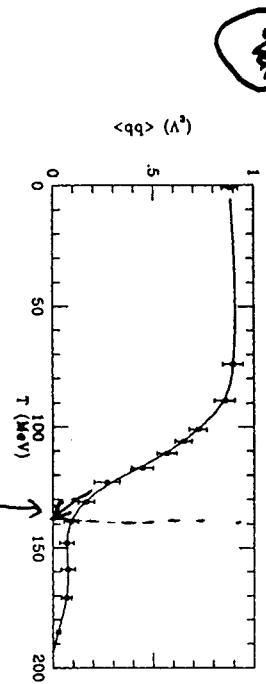
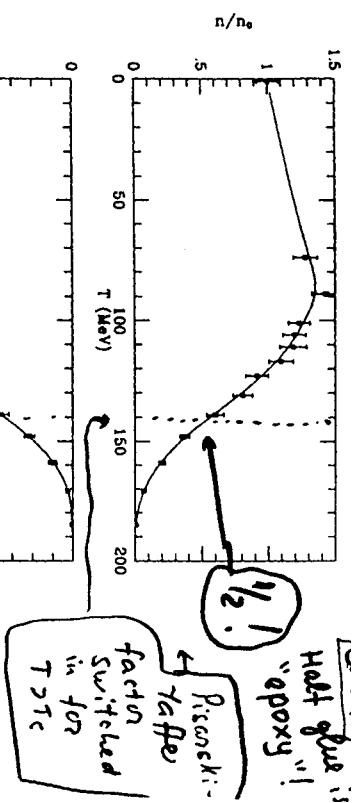


FIG. 9.

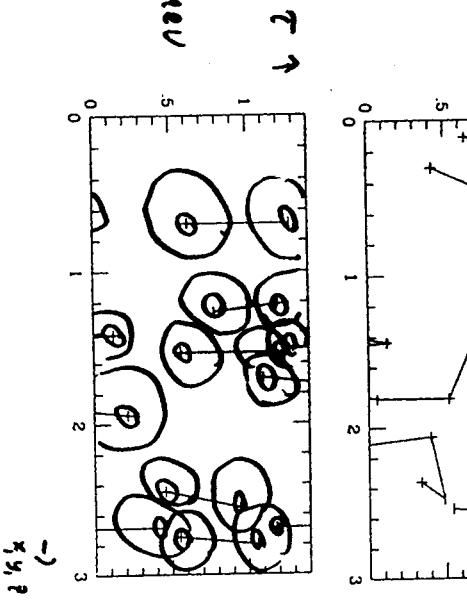
The quark condensate "melts"

at T = T_c, but the gluon one does not!

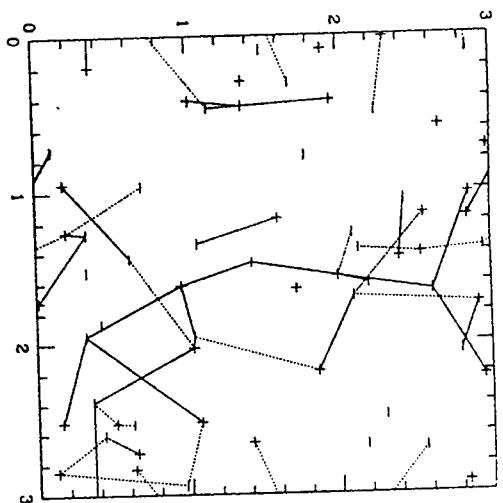
"Molecules" are the "epoxy"!

(glue which survives T_c!)

$$T = 123 \text{ MeV} \\ (\tau < \tau_c)$$



$$T = 158 \text{ MeV} \\ (\tau > \tau_c)$$



(13)

(14)

If instantons do not go away
at $T \gtrsim T_c$, what interactions
they produce?

$$\text{minider : at } T < T_c \quad \bar{u}_i \frac{\partial}{\partial t} \bar{u}_j \frac{\partial}{\partial t} \bar{u}_k \leftarrow \bar{\pi}$$

\uparrow
 $\text{'t Hooft}\text{-Lagrangian}$

+ violates $U(1) \Rightarrow \pi$ and η' correlators, etc
are very different, etc

"decreases" produce other interactions

$\mathcal{L} = G \left[\frac{2}{N_c^2} \left[(\bar{\pi} \tau^a \pi)^2 - (\bar{\pi} \tau^a \eta' \psi)^2 \right] - (\bar{\pi} \tau^a \delta_0 \psi)^2 - (\bar{\pi} \tau^a \delta_0 \psi)^2 \right]$

$\sim \# \text{ of molecules}$

$\sim \frac{2^4}{N_c^2} (\bar{\pi} \delta_0 \delta_0 \psi)^2 \}$

In general, NJL-type lagrangian at $T \neq 0$ has \neq possible structures..., this has fixed factors η symmetric \Rightarrow attractive for $(\bar{\pi}, \delta)$, (η, δ) channels

Traceless η, A_μ are not affected

50's BCS...
60's Gorkov-Grempel
70's QGP, string

Brief history

- 70-80's: Quarks of different colors are attracted perturbatively: S.
- C. Frautschi (Eric1978), F. Barrois, Nucl. Phys. B129, 390 (1977), D. Bailin and A. Love, Phys. Rep. 107, 325 (1984). $\Delta \sim \text{MeV}$ only...

- T. Schaefer, E.S.J. Verbaarschot Nucl. Phys. B412, 143 (1994): ud scalar diquarks are very deeply bound in the instanton model, being a very robust element of Nucleons (octet) baryons, as opposed to Δ (decuplet) ones. Sorry: too many phenomenological hints to mention here: weak decays, formfactors, fluctuations of the N cross section...

- First attempts to study instantons at finite density numerically T. Schäfer, Phys. Rev D57 (1998) 3950.: diquarks persist, even at high μ : "polygons"

- Two papers (submitted to hep-ph on the same day) about instanton-driven superconductivity for $N_f = 2, N_c = 3$ appear: R. Rapp, T. Schäfer, E. V. Shuryak and M. Velkovsky (RSSV) Phys. Rev. Lett. 81 (1998) 53. M. Alford, K. Rajagopal and F. Wilczek (ARW) Phys. Lett. B422 247 (1998).
: large condensate $\Delta \sim 100 \text{ MeV}!$

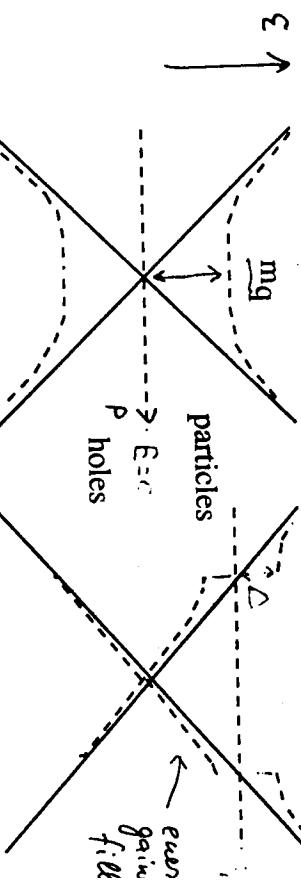
- Color-flavor locking is proposed and verified for OGE in ARW hep-ph/9804403. It is also preferred by instantons RSSV, hep-ph 9904353 (probably always true).

instantons RSSV, hep-ph 9904353 (probably always true).

- Magnetic gluons overtake electric ones at large μ , the condensate grows with μ D.T. Son, Phys. Rev. D59:094019, 1999; hep-ph/9812287

- Transition between two CSC phases, as m_s changes, is discontinuous: the first order RSSV, Schafer+Wilczek, Rajagopal + Berges 99. Finalized the phase diagram (the mean field).

Why transition from particle-hole to particle-particle pairing ?

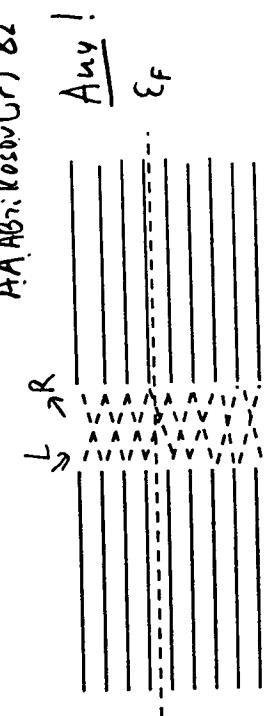


Energy versus momentum: the blue dashed line show the dispersion curve for vacuum and dense matter. It has discontinuity at two different places the surface of the Dirac sea and Fermi sphere.

* Cooper instabilities:
 Δ is helped by $\rho_{\text{eff}} = \dots$
 Any coupling works ...

Why instantons?

- It is the strongest non-perturbative effect generally → (talk at α_s , $\alpha_1, \alpha_2, \alpha_3$)
- Explains quantitatively chiral symmetry breaking in vacuum. Gap is large: ($m_{\text{constituent}} = 330 - 400 \text{ MeV}$)
- Anomaly is not eliminated by adding $\mu \gamma_4$ to the Dirac operator¹



- But at very high density instanton effect are suppressed by the Debye screening (E.S.1982)

$$dn(\rho, \mu) \approx d\exp(-N_f \rho^2 \mu^2)$$

¹ In random matrix models people have used a simple-minded approach: adding $\mu \gamma_4$ to the Dirac operator represented as a random matrix with some density of zero modes (leading to quark condensate). If μ is sufficiently large, eigenvalues move away from zero and chiral symmetry gets restored.

Instantons and triality

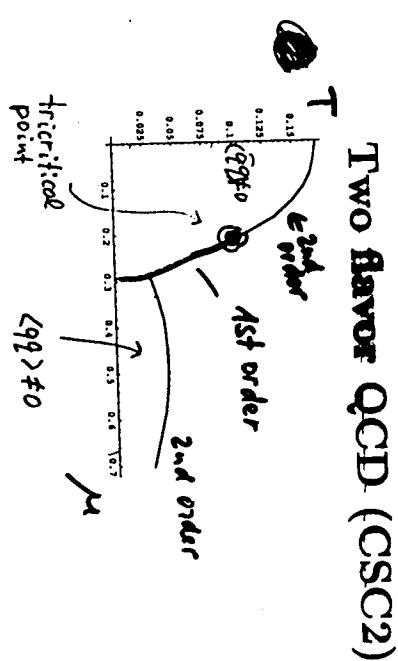
- There are three attractive channels, which compete
 - instanton-induced attraction in $\bar{q}q$ channel leads to χ -symmetry breaking, also γ'_1 mass - $U(1)$ problem
 - instanton-induced attraction in qq leads to color superconductivity, It decreases with N_c as $1/(N_c - 1)$ $\left[\begin{smallmatrix} \text{same} \\ \forall a \in QCD \end{smallmatrix} \right]$
 - light-quark-induced attraction of $\bar{I}I$ leads to pairing of instantons into “molecules”. effect increases with N_f

- The first two phases can be described by mean field Approx.
→ not the last!

Two colors: a very special theory

- The opposite to the large N_c limit:
Baryons are degenerate with mesons:
Pauli-Gursey symmetry (Unlike SUSY
different number)

- symmetry breaking is $SU(2N_f) \rightarrow Sp(2N_f)$ For $N_f = 2$ the coset $K = SU(4)/Sp(4) = SO(6)/SO(5) = S^5$: 5 massless modes: pions plus scalar diquark S and its anti-particle \bar{S}
- RSSV1: finite μ breaks rotates the 5-dim sphere. Scalar diquark (not sigma meson) becomes massive. more in: Kogut, Stephanov and Toublan hep-ph/9906346
- Fermionic determinant is real: lattice simulations possible. Results by Karsh, Dagotto et al of mid-80's make sense! See recent work by S.Hands et al.



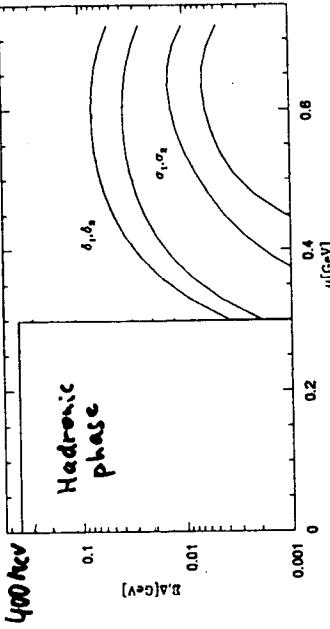
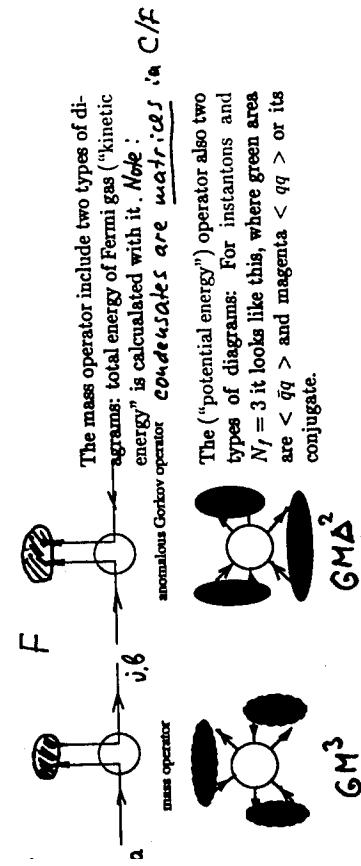
Schematic (simple form factor in 3-mo instanton-induced lagrangian

The phase diagram from Berges Rajagopal: Similar diagrams: RSS Diakonov and Carter,Klevansky et al.

Three flavor QCD (CSC3)

$m_i = 0$ chiral limit

how the calculations are done:
the mean field way



Then one minimizes the sum and get
gap equations There are many because
all masses/condensates are color-flavor
matrices.

Approximations: (i) The coupling
constant G is treated as constant.
(ii) No clustering included.

Color flavor locking (ARW2) is preferred by one-gluon-exchange
 $\langle q_i^a C q_j^b \rangle = \bar{\Delta}_1 \delta_{ia} \delta_{bj} + \bar{\Delta}_2 \delta_{ib} \delta_{ja}$
 $SU(3)_c SU(3)_f \rightarrow SU(3)_{diagonal}$
 More complicated calculations (RSSV)
 show that instantons prefer it as
well (and $\Delta_1 = -\Delta_2$)

The “continuity” issue

T.Schafer and F.Wilczek (98) pointed out that CSC3 phase has not only the same (?) symmetries as hadronic matter, but also very similar excitations:

The condensates conveniently mix

color with flavor	hadronic language	comment
quark language	8 massive vect. mes.	Meissner eff.
8 gluons	8+1 “baryons”	$\Lambda(1405)$? if $<\bar{q}q> \neq 0$
3*3 quarks	remain!	
8 massless pions	massless γ_{inside}	like γZ in SM
γ is combined with “hypercharge” g		???
Singlet scalar $U^{(1)}_b$ -H condensate		



But: It is still not transparent for

Magnetic ones got no screening at $T=0$ (One has also to take care of time delay effects, since we now speak of relativistic bound state bound by exchanges of propagating quanta... Elia berg eqn.)

T.D.Son, hep-ph/9812287 therefore f

γ_{outside} (something Weinberg/Salam should not have worried about) so it will levitate in an ordinary magnet, or reflect light from the surface...

→ Is it the correct condensation pattern of $N_f = 3$ nuclear matter?

(25)

The one-gluon exchange

The operator $(\gamma_\mu t^a)(\gamma_\mu t^a)$: no chirality flip

Strength depends on momentum transfer Q (it is after all the Rutherford-like scattering)

Electric exchanges are Debye screened at $Q \sim g\mu$ (like instantons)

at $Q \sim g\mu$ (like instantons)

only Landau-damping

(One has also to take care of time delay effects, since we now speak of relativistic bound state bound by exchanges of propagating quanta... Elia

berg eqn.)

a “double log” in the gap equation

$1 = \text{const } g^2 \log^2 \Delta$ | ^{one log} → the other thus unusual answer: $\Delta \sim \mu \exp(-\frac{3\pi^2}{\sqrt{2g}})$

→ γ_{inside} (something Weinberg/Salam should not have worried about) so it will levitate in an ordinary magnet, or reflect light from the surface...

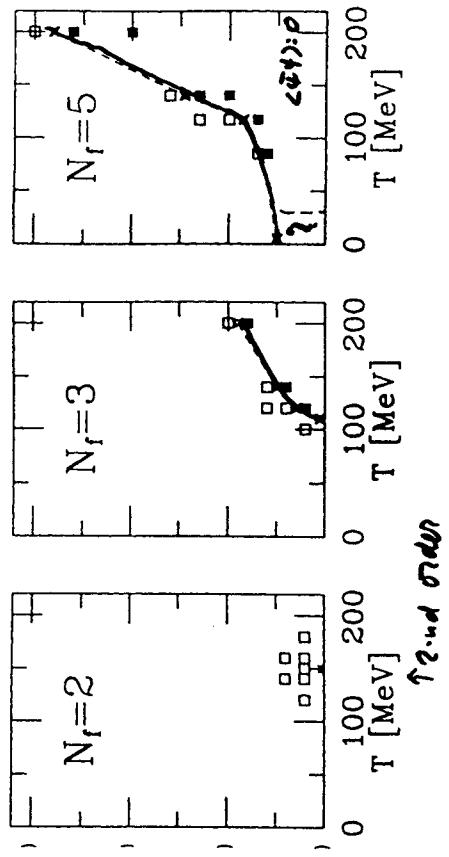
Is it the correct condensation pattern of $N_f = 3$ nuclear matter?

(26)

T. Schäfer
f. Bouyoucos
T. D. Son

Magnetic Equations

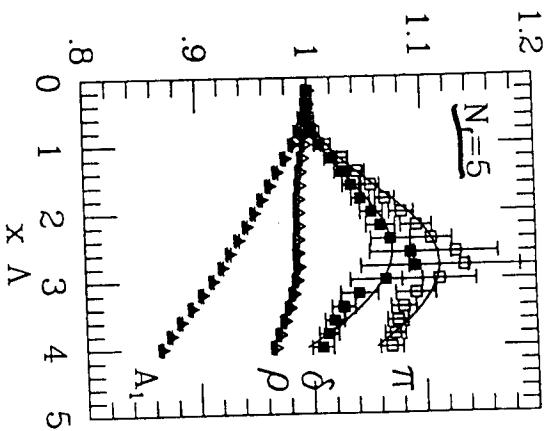
FIG. 7.



T. Schäfer LS. 95

Are there bound states in the chirally symmetric phase?

Conclusions



$m_{\text{quark}} = 0.1 \Lambda$
used (and fitted
from the correlations)

\Rightarrow So chiral sym.
is not exact

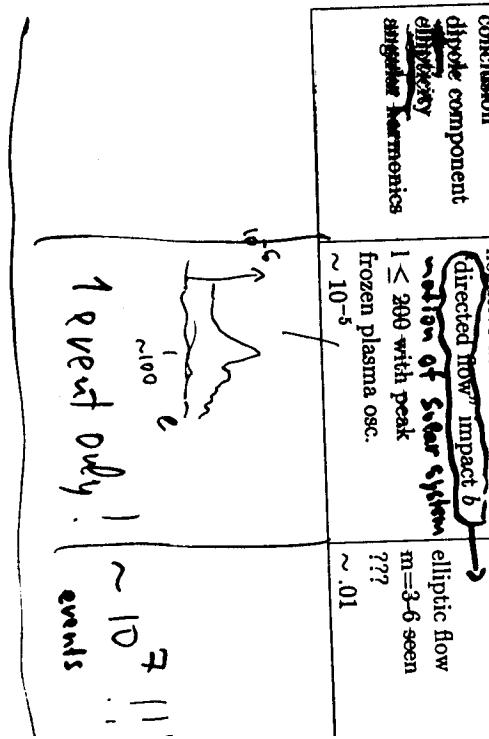
- The vacuum/hadrons are in the chirally broken phase, with $\langle \bar{q}q \rangle$ condensate generated by Redinstants
 - At high $T > T_c \approx 160 MeV$ the Redcondensate melts: QGP
 - At low T and high density Col Superconductivity is expected, with $\langle \bar{q}q \rangle$ condensate, also generated by instantons
 - Chiral symmetry first disappears in the SCS2 and then reappear again in CFL phase.
 - It persists till indefinitely large densities, with magnetically bound Cooper pairs. The gap grows large μ
- Yes: $m_\pi = m_\delta = m_\sigma = m_{\eta'} = \dots$
 $= 1.4 \Lambda (\pm 0.3 \Lambda)$ are consistent
 All other channels (N, \dots) are consistent
 with free quarks

Lecture 2: Heavy Ion collisions: the Quark-Gluon Plasma search

- - **Prolog:** Little Bang vs. the Big One
- - The final state: observed spectra and phase diagram
- - Radial and elliptic flows
- - The "initial" state: has QGP been discovered at CERN?
- - Dileptons: looking directly into hot matter
- - The J/ψ , ψ' and ϕ stories

Two explosions: the Big Bang versus the Little one

	Big Bang	Little Bang
expansion visible T	Hubble law $v \sim r$ 3K today, ~ 1 eV	same but anisotropic 170 MeV chemical
The final velocities status	at freeze-out Hubble constant, recently fixed to 10%	110-140 MeV thermal
acceleration history conclusion	distant supernovae negative acceleration now?	final radial flow
dipole component ellipticity	directed now? impact b	$v_t = .5 - .6$
angular harmonics	<u>rotation of solar system</u> $l \leq 200$ with peak frozen plasma osc.	Ω -flow accelerates  at the
	$\sim 10^{-5}$	elliptic flow $m=3-6$ seen ??? $\sim .01$



Z

Why study heavy ion collisions?

e.g. to see what happens with vacuum
and hadrons near the phase transition

Elementary mechanics of a fireball

$$\begin{aligned} \text{kin} &\sim \left(= \text{very big MIT bag} \right) \\ QGP &\sim \left(\frac{(16+3.322)\pi^2}{3} \right) \text{ adds to vac.} \\ &\sim \varepsilon : \left[(\# \text{DOF}) \text{ const. } T + B \right] \\ &\sim p : \left[(\# \text{DOF}) \text{ const. } T^4 - B \right] \end{aligned}$$

expands against the vacuum present

1 GeV/fm^3 ($B_{\text{ext}} \sim 50 \text{ MeV fm}^{-3}$)
very diff. between (That's why we
and pert. vacua) \leftarrow need QMTC!

atmospheric pressure, which is seen off one
a pump the air out, it is seen only if we go to
new phase, $\frac{\partial \rho}{\epsilon} = \frac{1}{\text{const. (DOF)}} T^4 - B$

(is produced by \rightarrow
mass to be moved is \rightarrow)

$\left\{ \text{makes the EOS softer}\right.$

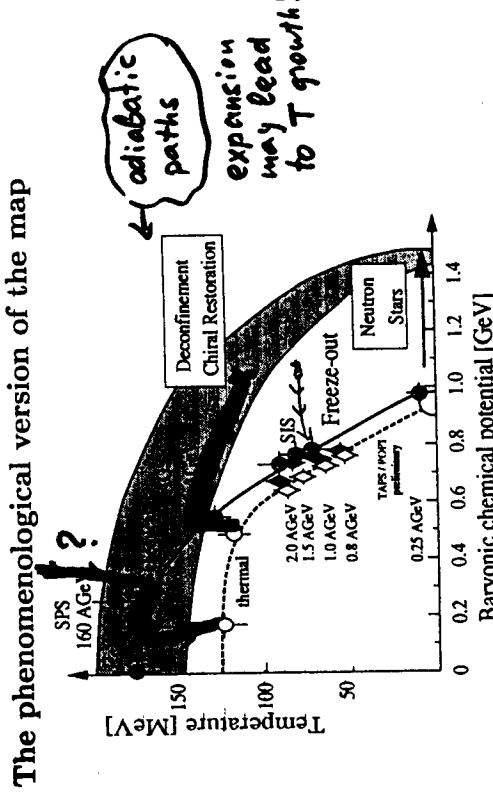


Figure 1: Solid (dashed) lines indicate chemical (thermal) freeze-out. Adopted from U. Heinz, hep-ph/9902424; The paths ... are from C.M.Hung, E. Shuryak, Phys.Rev.C57:1891-1906,1998

- Looking backward in time, from data one can identify “chemical” and “thermal” freeze-outs.
- So we did find a new phase of matter at SPS, never seen before ! It is chemically frozen but kinetically equilibrated “resonance” gas.
- $\int \frac{dp}{E} = \text{const.}$, even in event generators, and close to thermal one
 - \rightarrow e.g. talk by L.Bruna on UrQMD at QM99
- Maybe non-equilibrium, but quite adiabatic !

Particle composition

- Looking backward in time, from detector, is like looking at the Sun: $T \sim 6000^0$ only, although it is hotter inside... “thermal” freeze-out.



- one can also identify “chemical” freeze-out from particle ratios

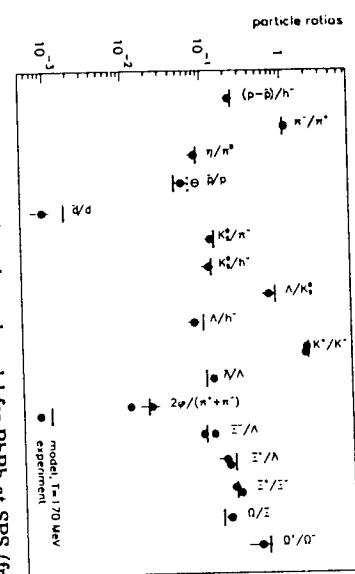


Figure 1: The ratios fitted to thermal model for PbPb at SPS (from J.Stachel)

hadronic chemistry	quark chemistry
fits many ratios very well	more parameters
$T \approx 170 - 190 MeV$,	fugacities (opposite for $\bar{q}q$)
s quark suppression: small in PbPb	and “phase space occupancies”
Problems:	(same for $\bar{q}q$)
why so high T ? ($\approx T_c$!)	
Can hadronic phase coexist?	
Why vacuum masses are used?	

How hot is matter at the beginning?
in heavy ion collisions?

5

Is there such thing as a collective
Pre-prehistory: Ancient debates
if the AA spectra are just a superposition of NN's: different mass slopes

- “Initial state” parton rescattering? No, the final state rescattering of hadrons - e.g. deuterons

- m_t slopes depend linearly on particle mass: this supports common flow idea $\langle p_t^2 \rangle \approx T + \frac{m_t^2}{2}$

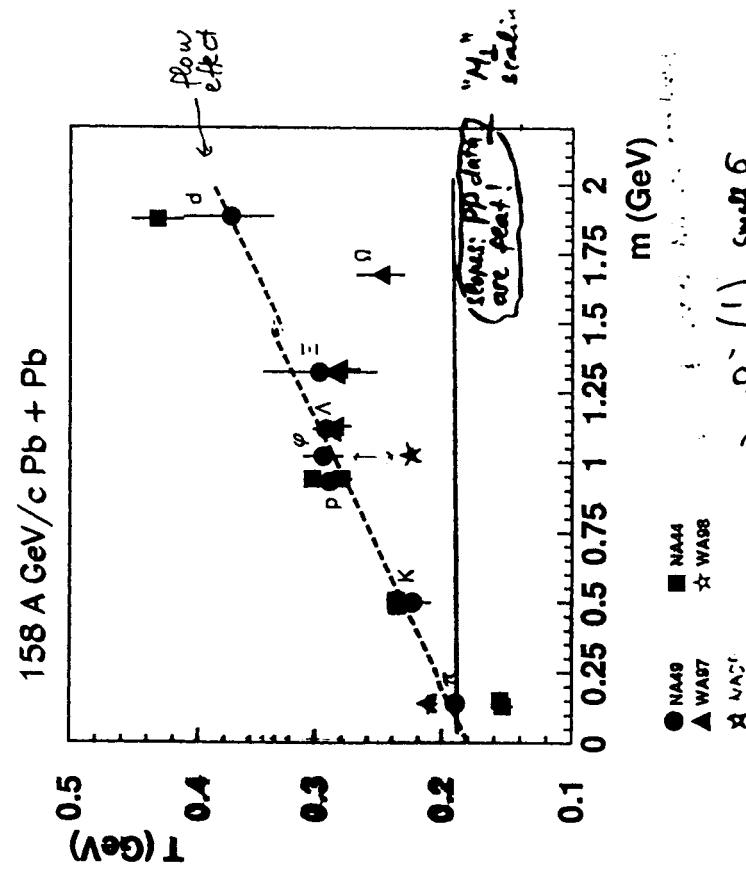
- “the larger the system, the further it cools” argument explains strong A and y dependence of v large $v_t \approx .6$ and low $T_f \approx 120 MeV$ in PbPb followed.

- Fit to NA49 HBT radii plus spe

6

tra had confirmed such v_t and T_f selection Heinz et al

mass dependence of inverse slopes



The softest point

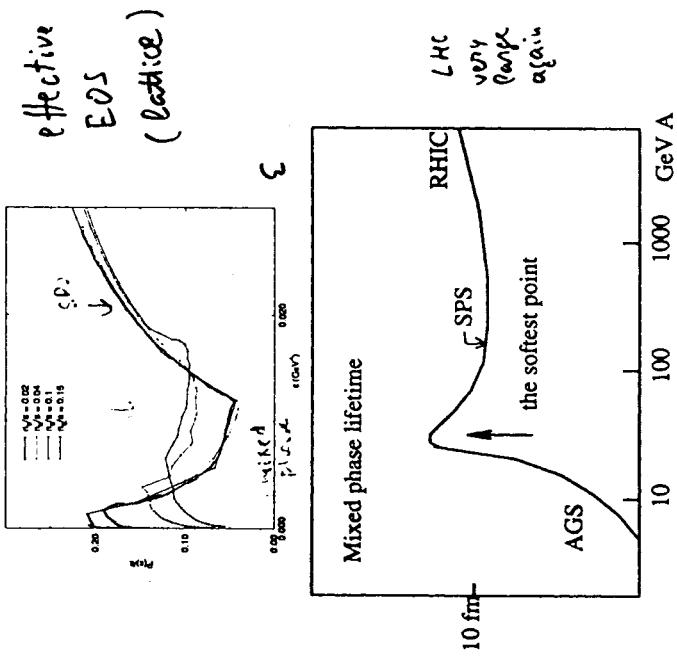
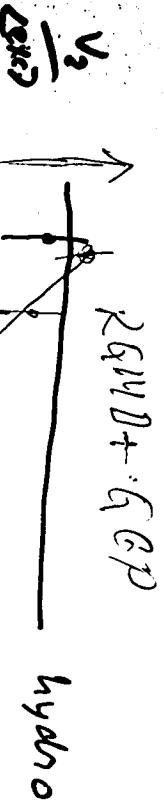


Figure 3: C.M.Hung, E. Shuryak, PRL 95

Next CERN SPS run is at 40 AGeV
 \rightarrow foot place in Oct 99

\rightarrow $\mathcal{R}^-(!)$ small
 \rightarrow $\varphi(?)$ K scale
 \rightarrow NA49 and NA50
 seem to see different slopes

Elliptic flow



Sorry, I have no time to discuss the "directed flow" or the dipole component... The picture of the "initial almond" for non-central collisions

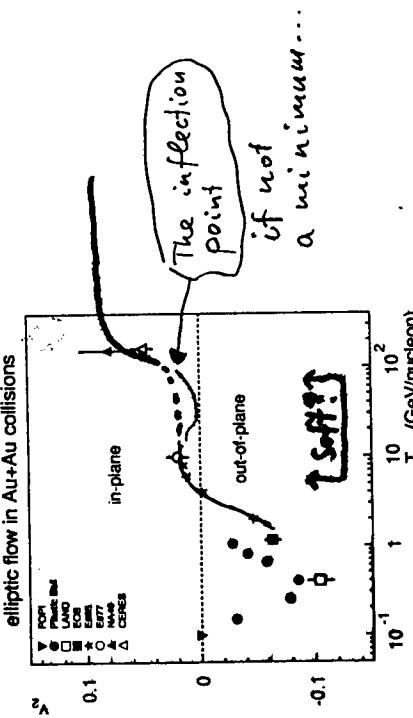
$$\frac{dN}{d\phi} = \frac{v_0}{2\pi} + \frac{v_2}{\pi} \cos(2\phi) + \frac{v_4}{\pi} \cos(4\phi) + \dots$$

- At low energies "squeeze-out" was observed in y direction, as spectators nuclei block the x direction.

WA49
SOURCE

- First hydro studies for AGS/SPS domain show significant v_2 in x direction Ollitrault Phys. Rev D46, 229(1992); Phys. Rev. D48, 1132(1993)
- elliptic flow is developed earlier than the radial one H Sorge, Phys. Rev. Lett. 78, 2309(1997). Furthermore, some interesting centrality dependence is found in H. Sorge, nucl th/9812057 (1998).
- Detailed calculations for AGS energies, with softening due to QCD phase transition P. Danielewicz et al., Phys. Rev Lett. 81, 2438(1998)
- At high (RHIC/LHC) energies more complex evolution in x-y plane is found (called the "nutcracker" scenario), with formation of two "shells" which are physically separated in direction D. Teaney and E. Shuryak, nucl-th/9904006 The v_2 does not grow with energy, but v_4, v_6 are predicted to grow!

- The status of experiments on elliptic flow can be summarized by the following figure:



Data selected
by J. Seward

EOS, Realistic vs.

- Illustration to softening of EOS at $E > 6$ GeV A

- Hydro** (and other event generators) seem to under-predict its value at mid-rapidity (compared to NA49 data): A QGP push already? (note however the error bars and the CERES point).

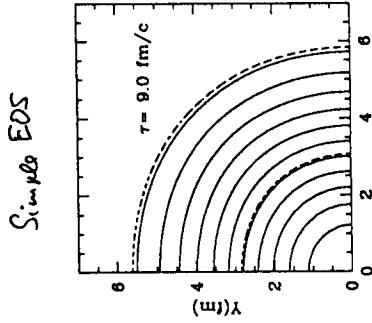
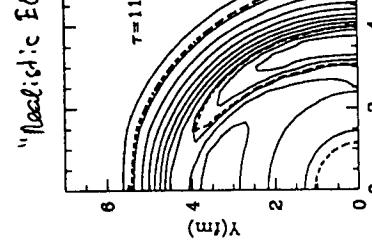
- Hydro calculations at higher energies D.Teaney and E.Shuryak, nucl-th/9904006 produce near constant ellipticity, which is rapidly switched off at SPS energies

- We may be lucky to see transition from soft to hard early EOS, inside the SPS energy domain, as an inflection point

RHIC as a nutcracker

- At RHIC we have to tell an orange from the nut
- Note that at CERN there is little difference with the initial shape
- Simple EOS $p = .2\epsilon$ of the resonance gas creates large expansion but basically preserves the elliptic shape

- “Realistic EOS” leads to formation of two shells, which then physically separate from each other! (The “nutcracker”)



D.Teaney + ES
nucl-th/9904006

DILEPTONS

The “initial” state: is there a QGP at SPS?

There are several important observations:

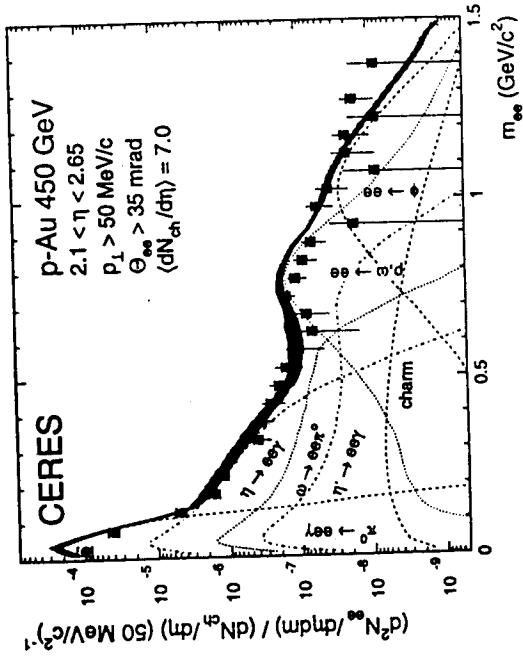
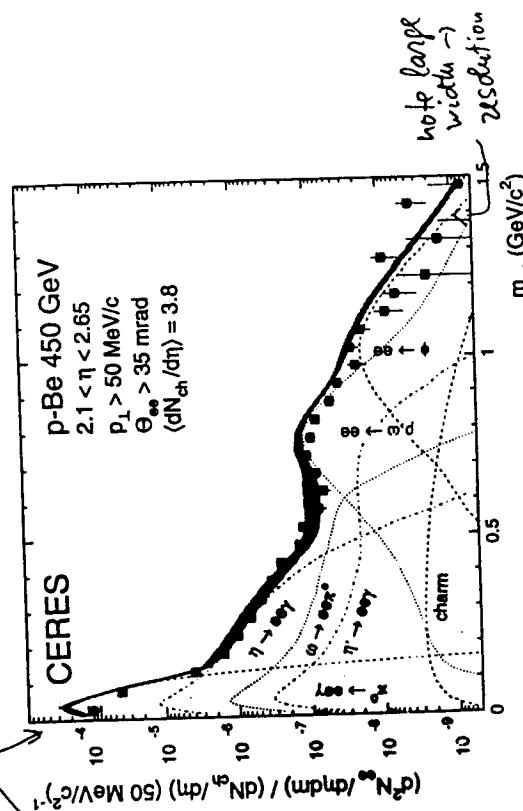
- Particle composition cannot be explained by reactions in hadronic phase, the fitted $T > 170 MeV$ – Is it indeed the QGP boundary?
- The initial EOS is very soft – QGP or strings?
- Dilepton production is enhanced and the spectrum is changed – approaching the QGP rates, or just complicated hadronic reactions?
- $J/\psi, \psi'$ production is further suppressed in central PbPb – Can we experimentally tell if it is not due to late hadronic absorption?

Old ideas: QCD phase transition causing “melting” of all hadrons ($\rho, \omega, \phi, J/\psi$). Dileptons are “penetrating probes”

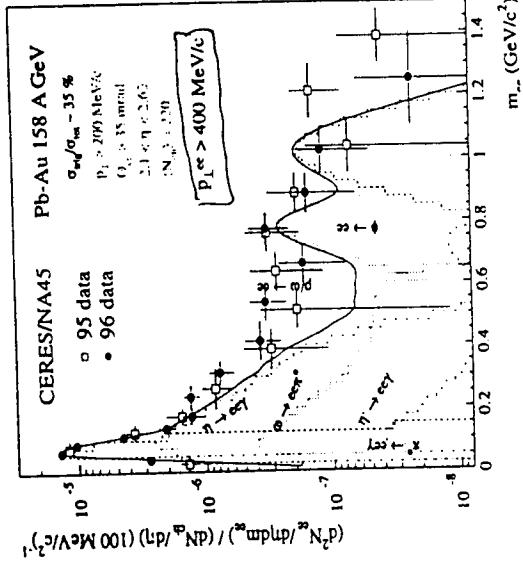
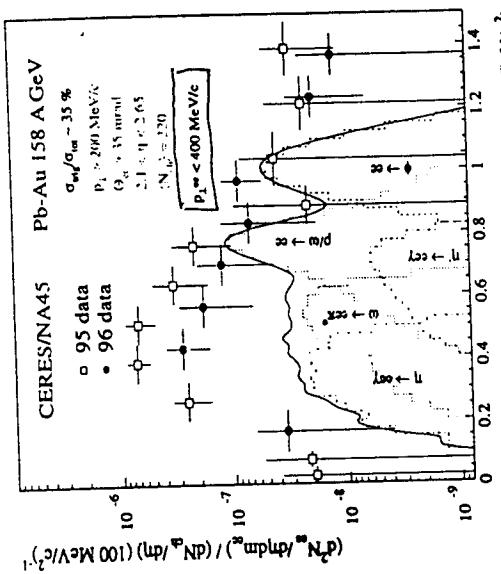
Good news: all dilepton experiments (HELIOS-3, CERES, NA50) see significant dilepton enhancement, compared to “naive” expectations. The effects are stronger at small p_t , clearly indicating matter effects
CERES sees qualitative change of sign of the vector spectral density for M_{ρ} as compared to the vacuum.

Bad news: Most radiation is not from QGP but from the “mixed phase” We still do not quite understand it More details are needed.

Previous CERES Results



e^+e^- pair mass spectrum



CERES

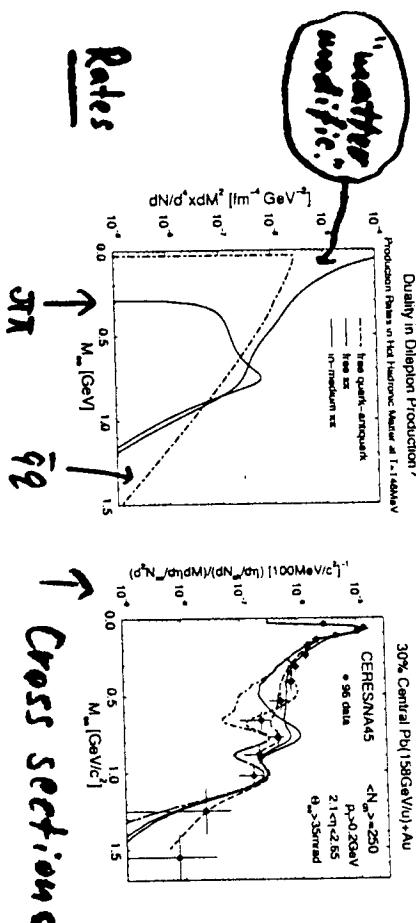


Figure 3: (Courtesy of Ralf Rapp) (a) Comparison of dilepton production rates: thermal pion gas, "partonic" (dash-dotted) "realistic" one (from Rapp et al.). (b) Comparison of CERES 96 data for mass spectrum of the observed dileptons with several theoretical calculations: no in-matter production (dash-dotted), no in-matter modification (solid with ρ/ω peak), the Brown-Rho scaling (dashed with a peak at $M \approx 5$ GeV), hadronic rho widening (solid) and pure "partonic" rate (dashed).

The main CERES-related physics issues are:

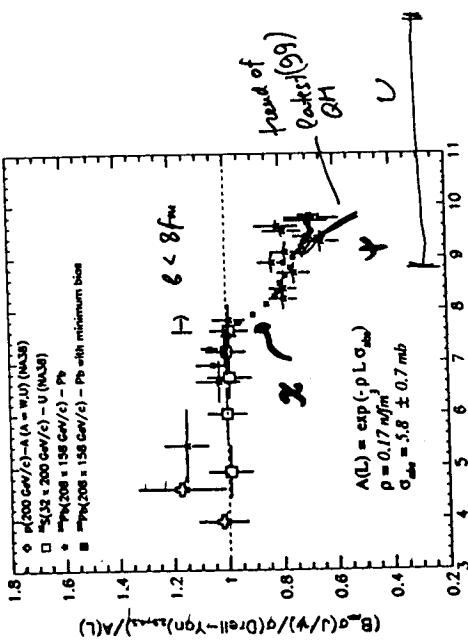
- (i) to what extent the observed " ρ melting" indicate approach of the chiral symmetry breaking,
- (ii) Does it really undercut the "resonance gas" picture (used in all event generators) ?

People who study/explain CERES data use vector meson masses shifted proportional to density with Walecka-type mean field model(G.Q. Li, C.M. Ko, G.E. Brown Nucl.Phys.A606:568-606,1996), or resonance re-scattering on hadrons, mostly excited nucleons (R. Rapp, G. Chanfray, J. Wambach Nucl.Phys.A617:472-495,1997)

My point here: Note also one striking fact: for the most important mass $M = .3 - .6\text{GeV}$ the "realistic" curve (obtained in a complicated hadronic based calculation) is not so far from the "partonic" one, which corresponds to just an ideal gas of quarks and antiquarks. So, we do find that the interaction between $\bar{q}q$ in the vector channel at $T \approx T_c$ is becoming weak.

Whatever the model, if vector spectral density is modified, the Weinberg-like sum rules (Kapusta,Shuryak 9 demand that the axial one also change. At chiral restoration they should coincide.

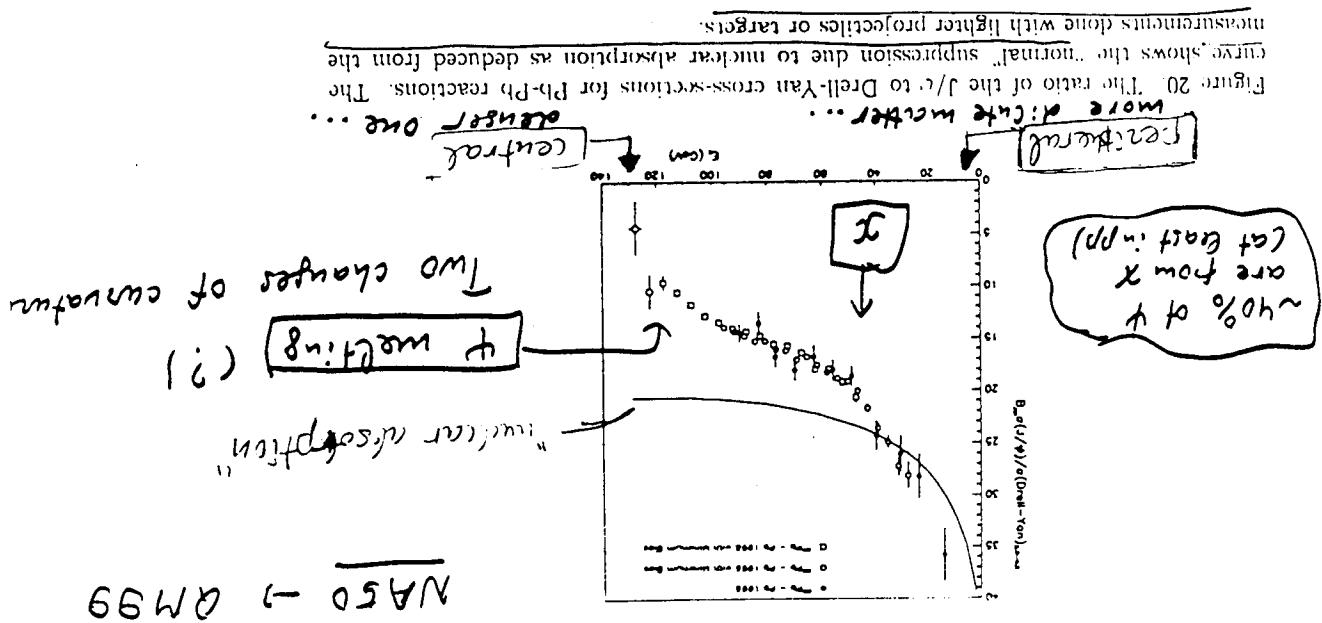
$J/\psi, \psi'$ SUPPRESSION



NA50 has found that PbPb collisions are different from pA-SS trend. Especially fascinating is rapid variation of suppression at centrality $ET \sim 50 \text{ GeV}$, or b>1 fm. More data needed, simpler target, or other A, or energy...

What is the mechanism of this change?
• gluonic photoeffect (Shuryak 78, Peshkin 80, Kharzeev, Satz, Nardi 95)

- the states in QGP simply do not exist (Matsui and Satz, 1986)
- hadronic comovers (Gavin and Vogt, Kahana and Kahana)
- change in the lifetime of the QGP due to the softest point (Shuryak and Teaney, 1998)



Conclusions

- - AA collisions produce a Bang not a fizzle. Radial flow at SPS develops late, mostly in hadronic phase.
- - Early “QGP push” is expected at RHIC, and maybe seen already at SPS in ellipticity (NA49)
- - At RHIC the non-central collisions leads to a “nutcracker”.
- - Dileptons see melting of ρ resonance and approach to “partonic rates” at small masses, or QGP-like radiation from hot matter
- - The J/ψ seem to be suppressed in steps: the only observable with strong A and centrality dependence. two components (χ, ψ)