

Physics Beyond the Standard Model — the Electroweak sector and more...

Tao Han

Univ. of Wisconsin - Madison

CTEQ Summer School, Madison (June 27, 2004)

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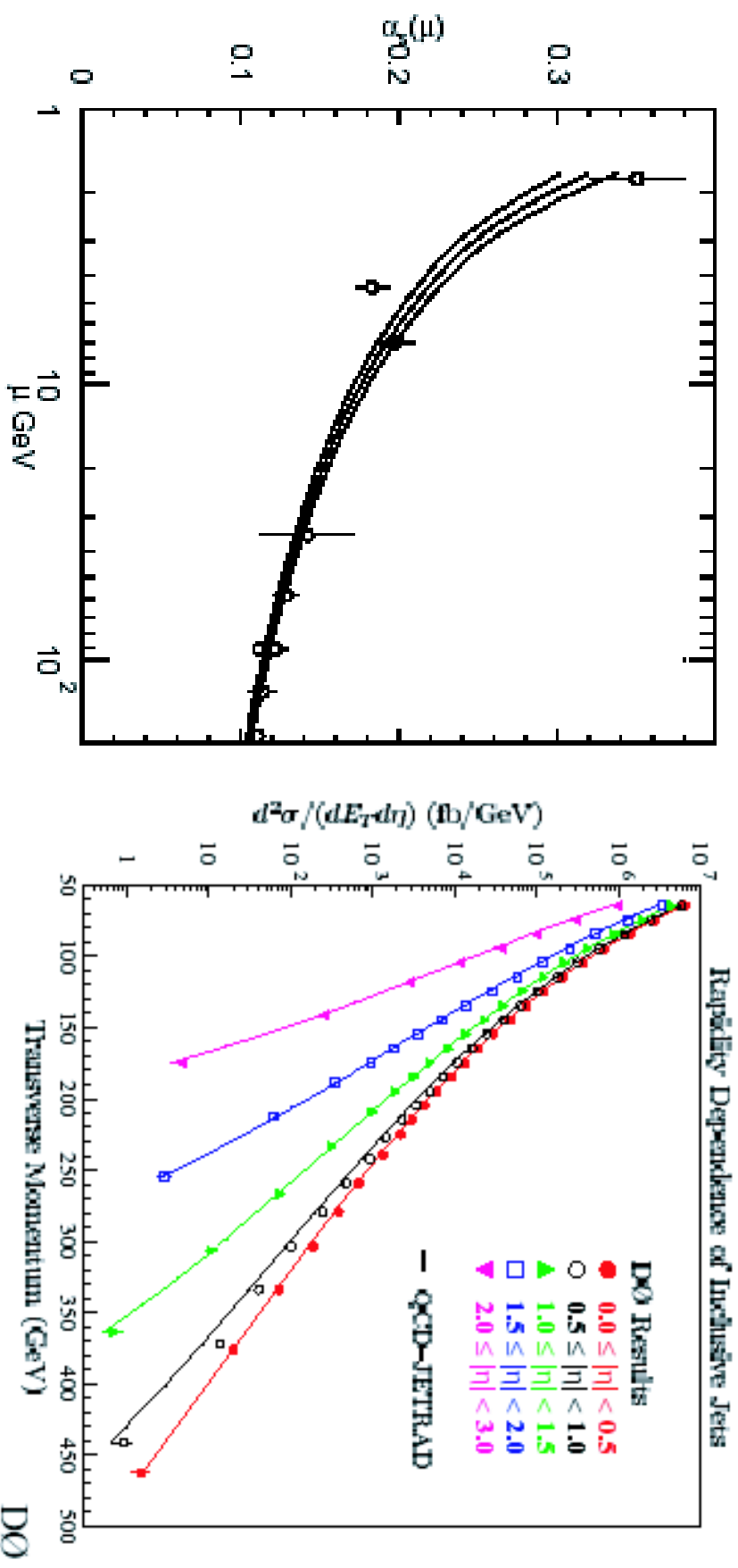
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The Standard Model as It Is
The Need For Going Beyond SM
Our “Theory Bank”
Their Signals at the LHC

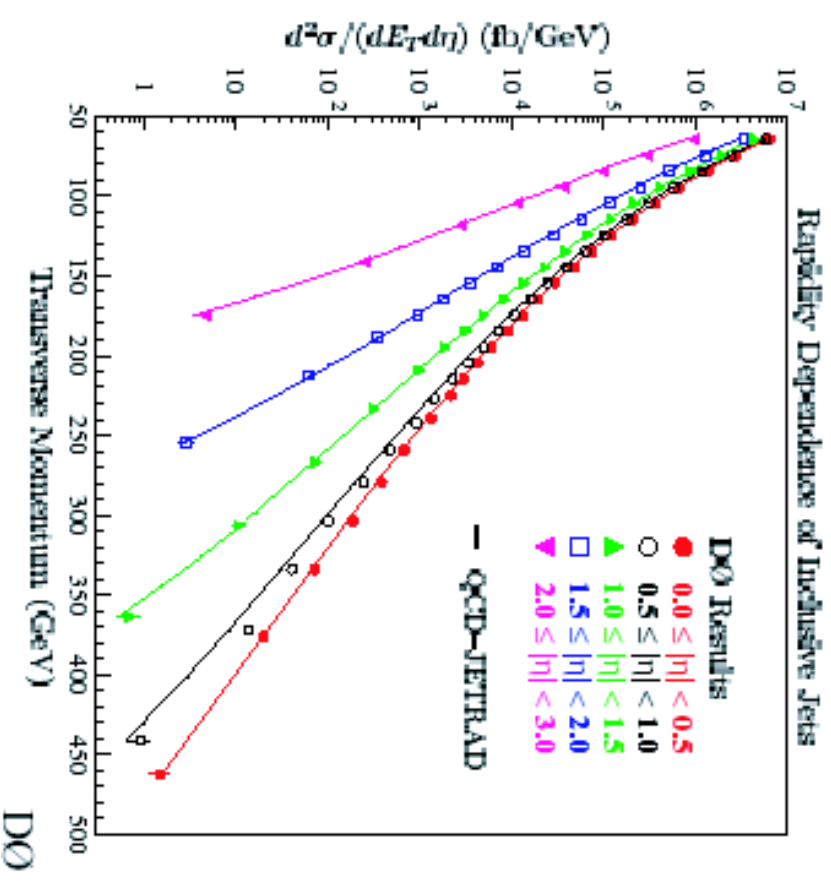
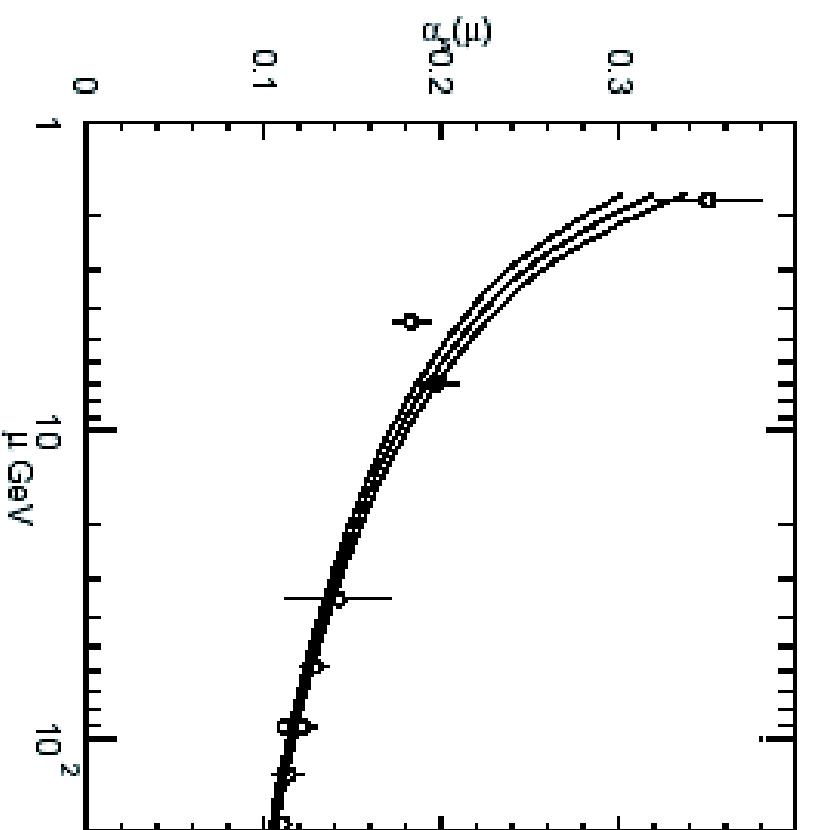
The Standard Model as a Low-Energy Effective Theory

- $SU_c(3)$ QCD as the theory of strong interactions:



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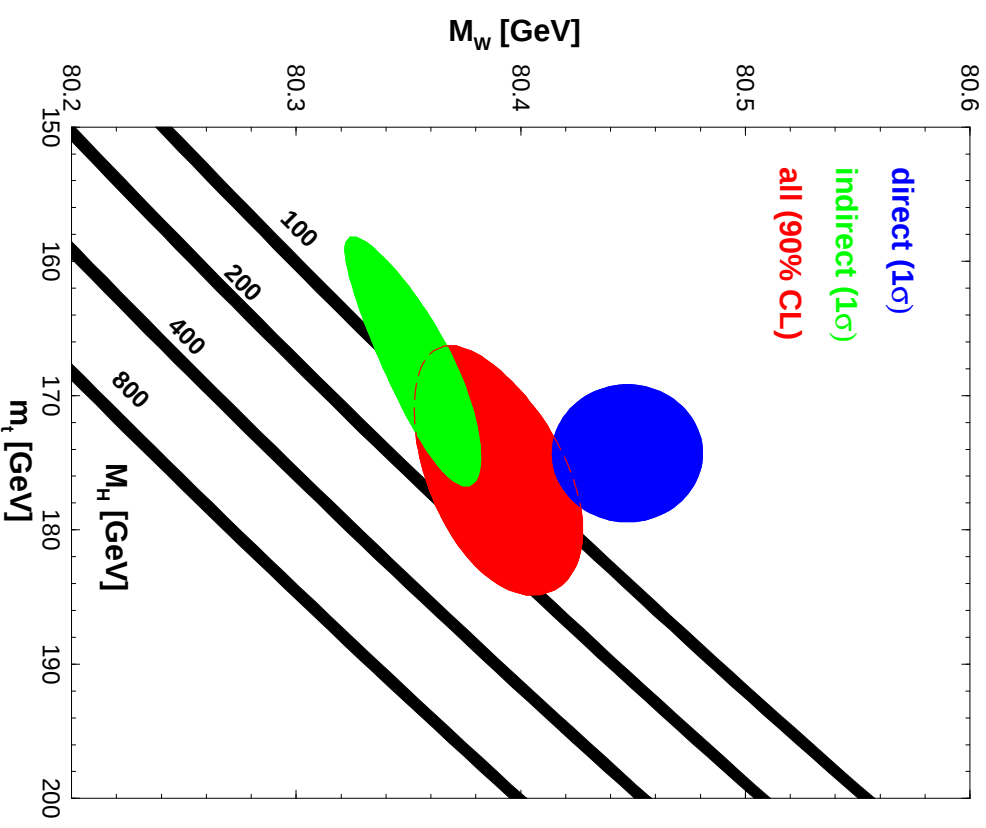
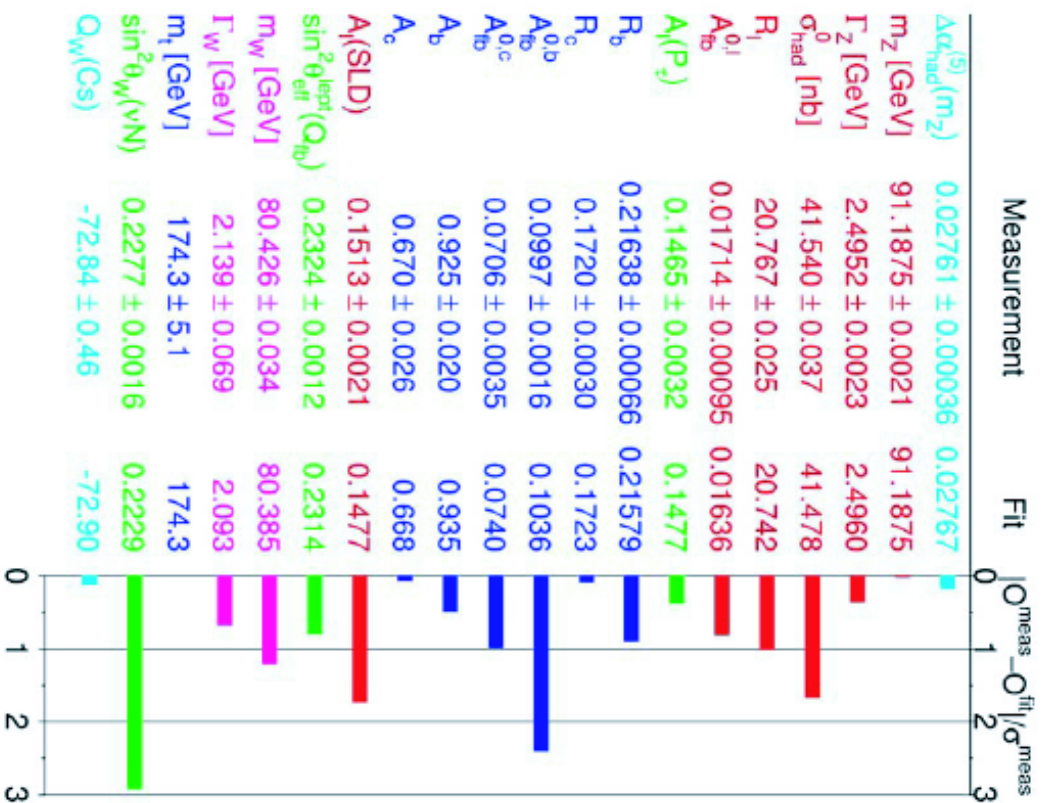
QCD remarkably successful:

Perturbative QCD well tested and formed foundation for HEP;

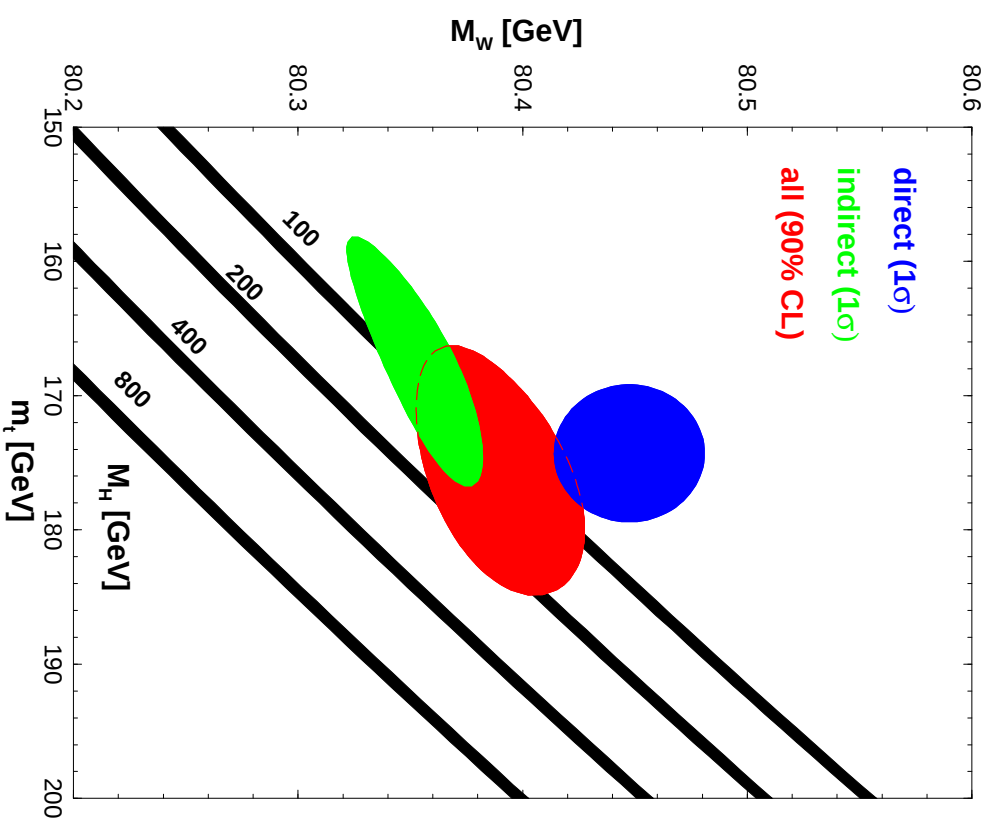
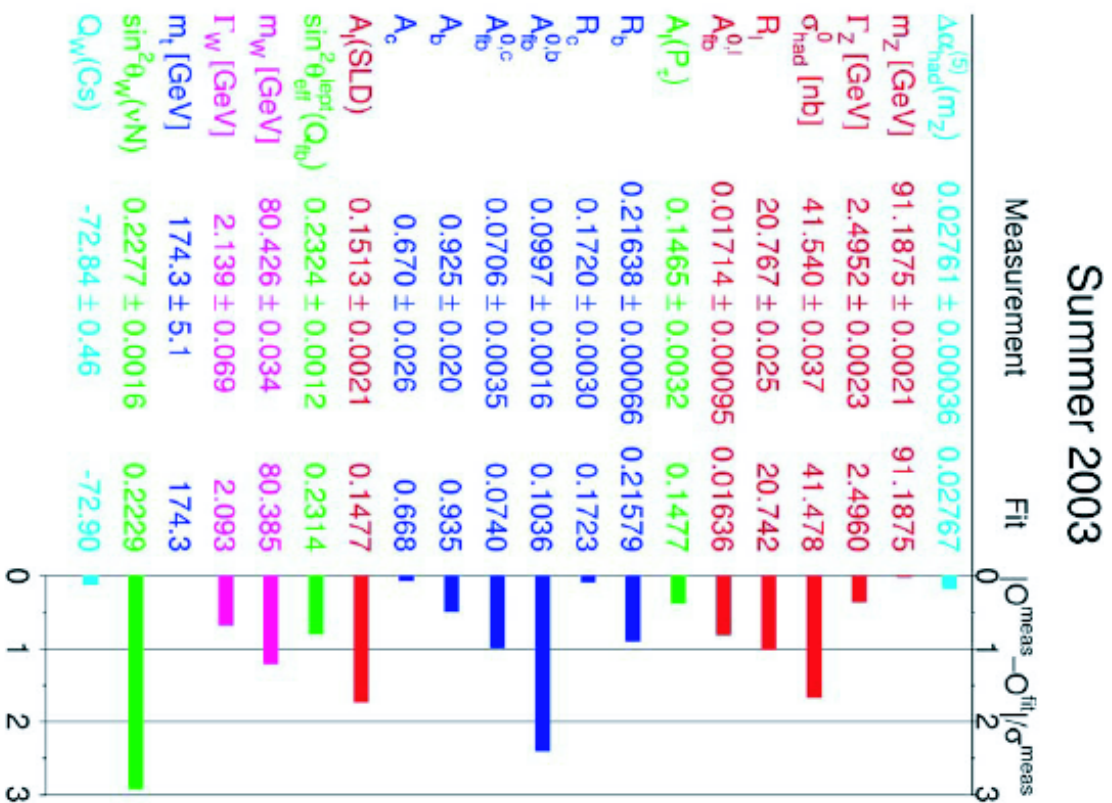
Significant progress in lattice gauge calculations.

- $SU_L(2) \otimes U_Y(1)$ EW theory and precision measurements:

Summer 2003



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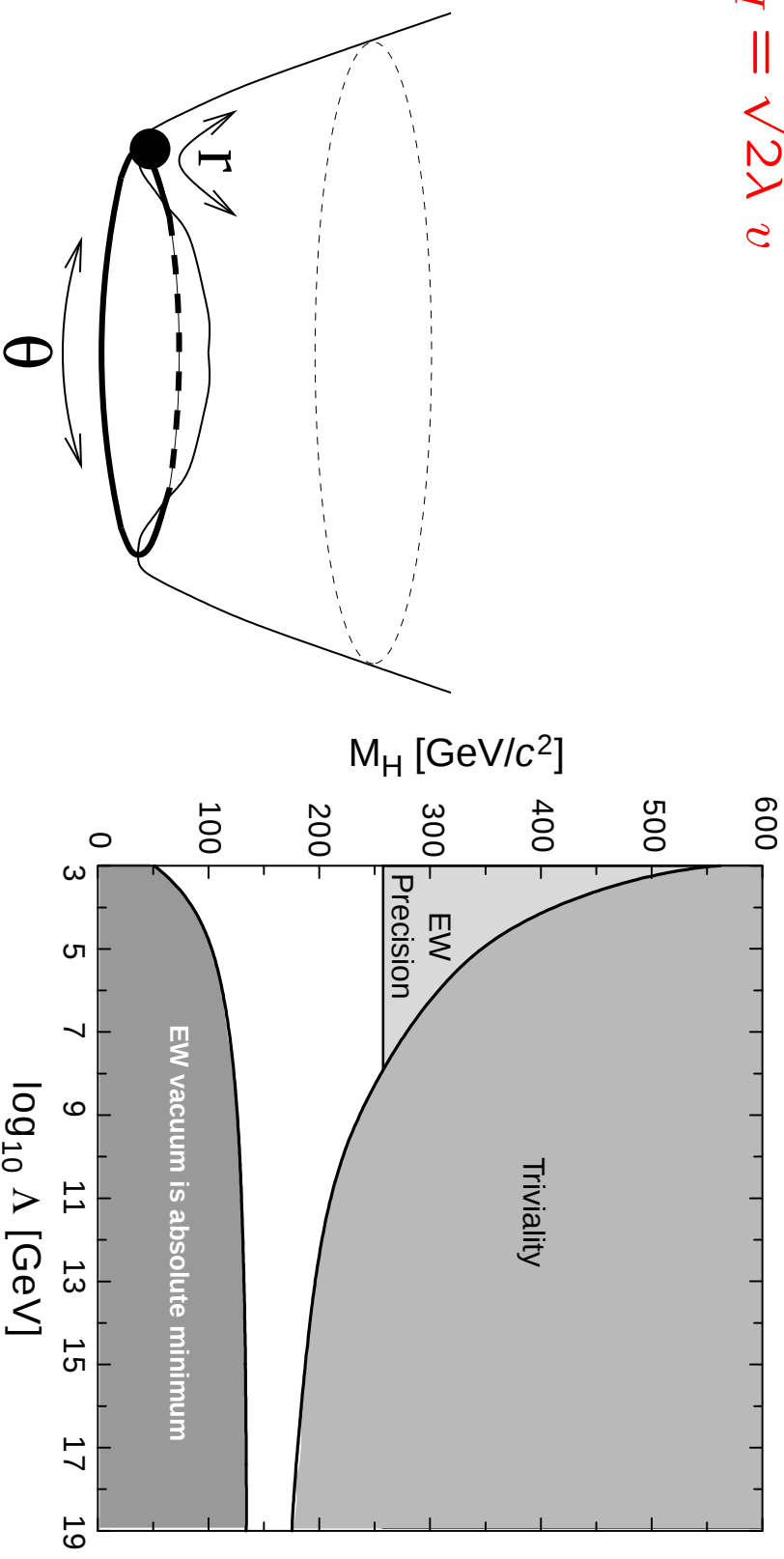


EW precision data: $m_H < 251$ GeV at 95% CL with $m_t = 178$ GeV.

- SM as an effective theory ?

$$V = -\mu^2 \Phi^2 + \lambda \Phi^4, \quad \langle \Phi \rangle = \frac{v}{\sqrt{2}} = \sqrt{\frac{\mu^2}{2\lambda}}, \quad v^{-2} = \sqrt{2} G_F$$

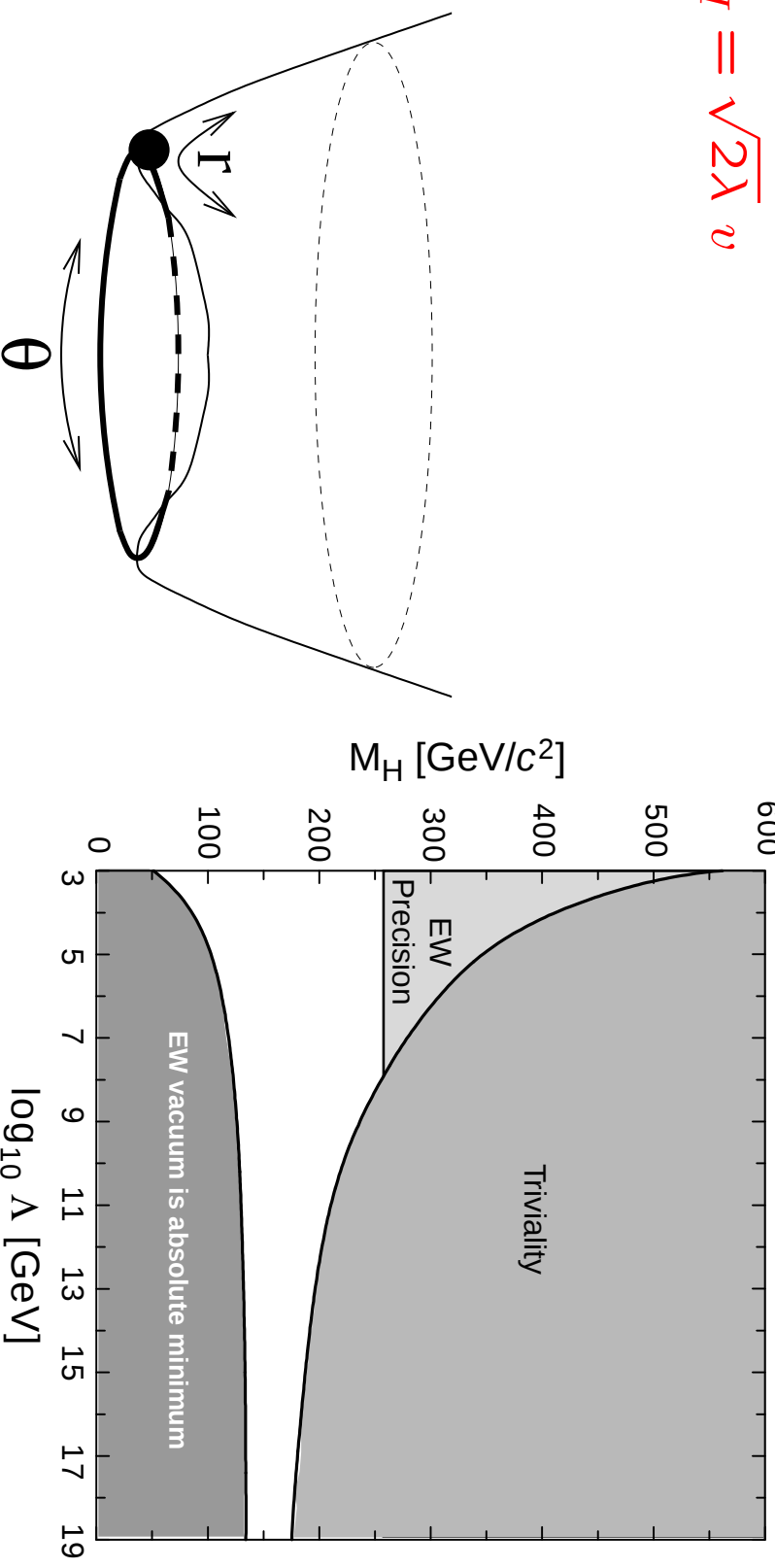
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$$m_H = \sqrt{2\lambda} v$$



All couplings $g_{2,3}$, $\sin^2\theta_W$, g_f and masses $\sim g_i v$ are in place.
 SM with a light H could be an *effective theory* to $\Lambda \sim M_{pl}$.

a stable vacuum;
 non-trivial interactions;
 renormalizability ...

Q: *Would you need physics beyond the Standard Model?*

A:



(The Garden of Eden)

The Need For Going Beyond SM ?

Vastly Separated Scales for Fundamental Interactions:

- QCD condensate: f_π

At the scale Λ_{QCD} , the interaction becomes non-perturbative:

$$f_\pi \propto \langle \bar{q}_L q_R \rangle_0^{1/3} \sim 100 \text{ MeV}.$$

Perfectly natural! We understand the dynamics.

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Empirically (Fermi's weak interaction) and theoretically (EWSB):

$$v = \frac{1}{(\sqrt{2} G_F)^{1/2}} = \frac{2M_W}{g} \approx 250 \text{ GeV}.$$

We do NOT know the underlining dynamics!

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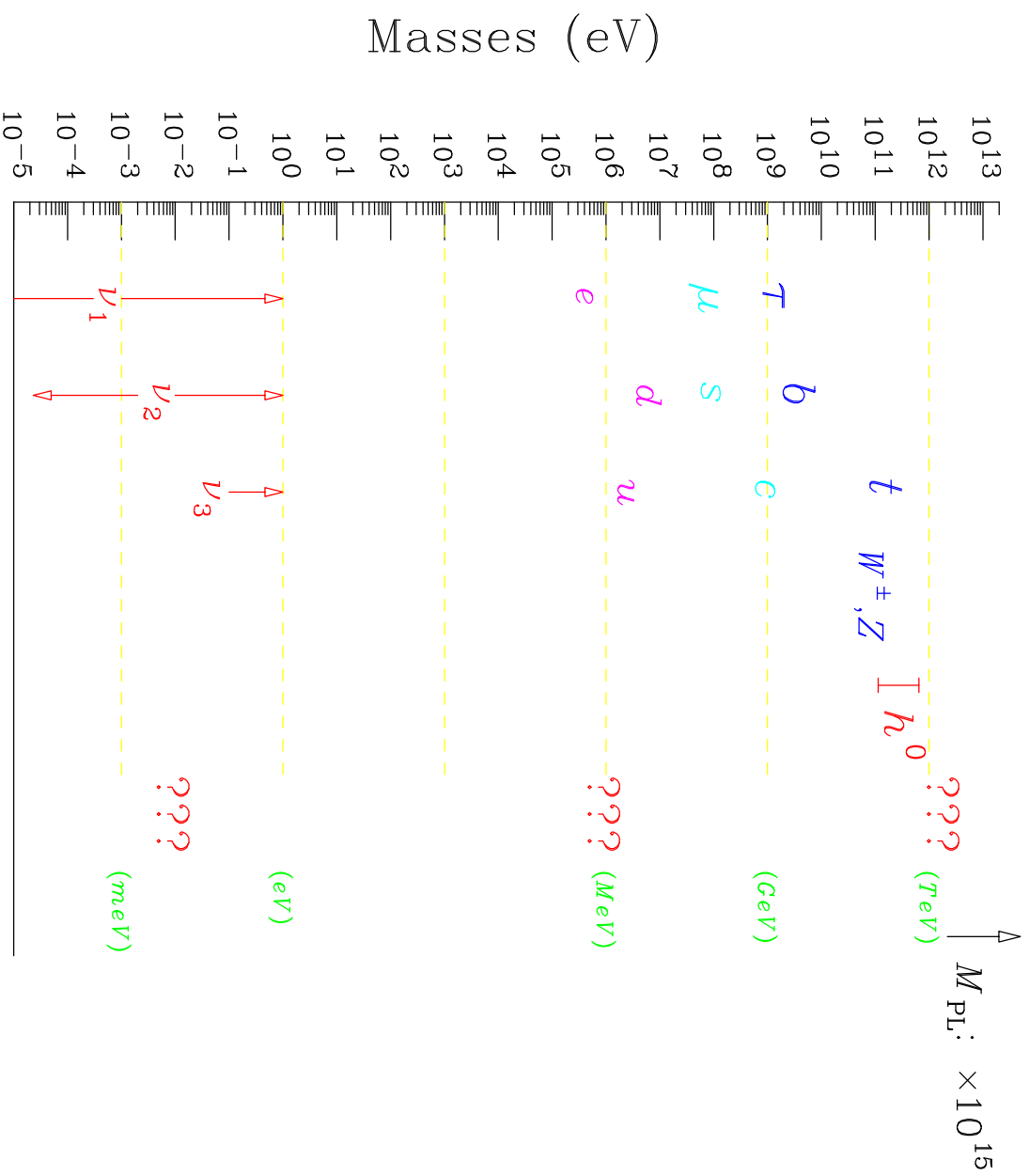
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- Quantum Gravity?

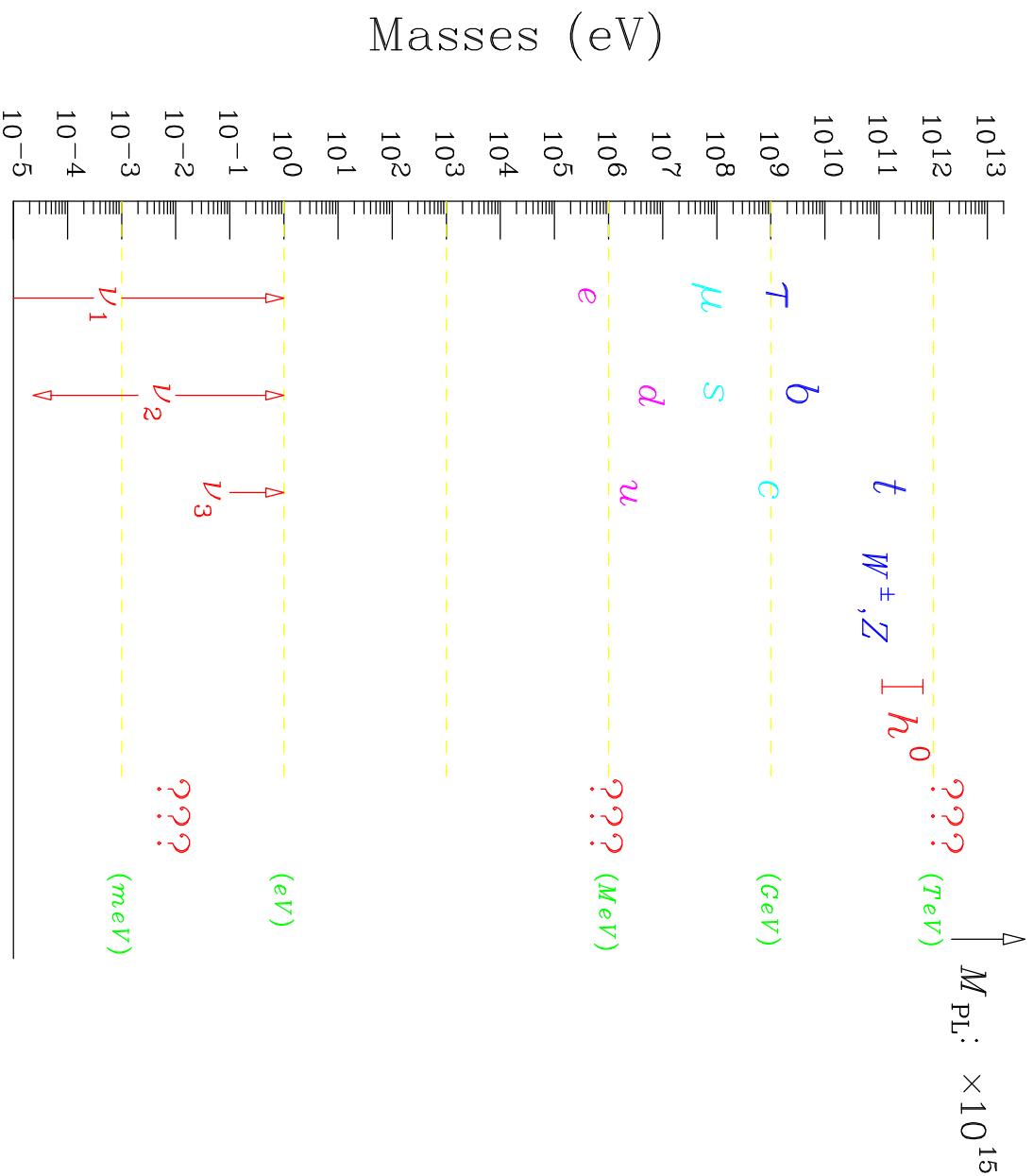
$$M_{Pl} = \frac{\hbar c}{\sqrt{G_N}} \approx 10^{19} \text{ GeV}.$$

We have NO clue about it ...

Mass Spectrum in a Wide Range:



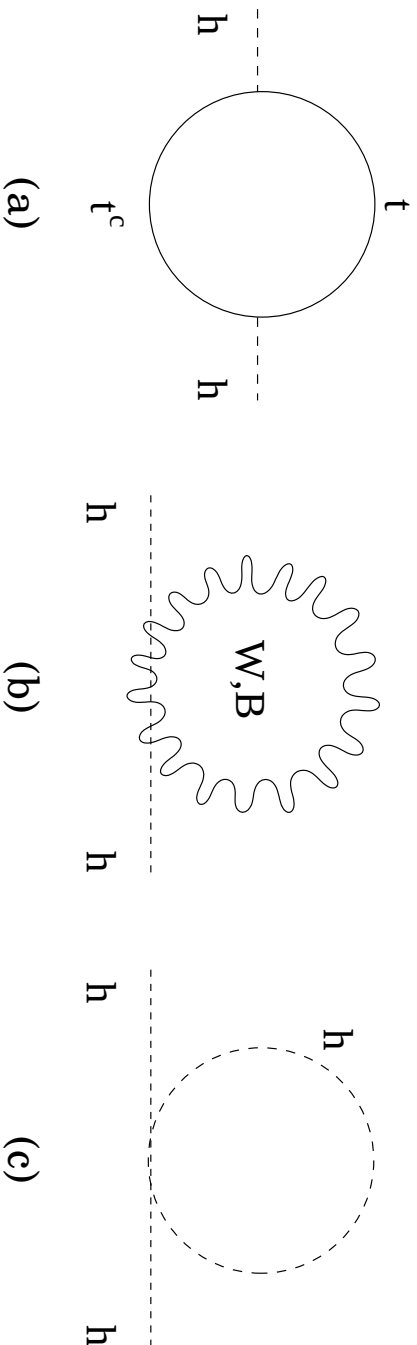
Mass Spectrum in a Wide Range:



EW scale: $v \approx \mathcal{O}(1 \text{ TeV})$; $m_\nu : 10^{-15}$ down ? $M_{pl} : 10^{15}$ up ?.

The Large Hierarchy: all way up to M_{pl}

Due to quantum corrections, the Higgs mass is quadratically sensitive to the cutoff scale: $\sim \Lambda^2$.

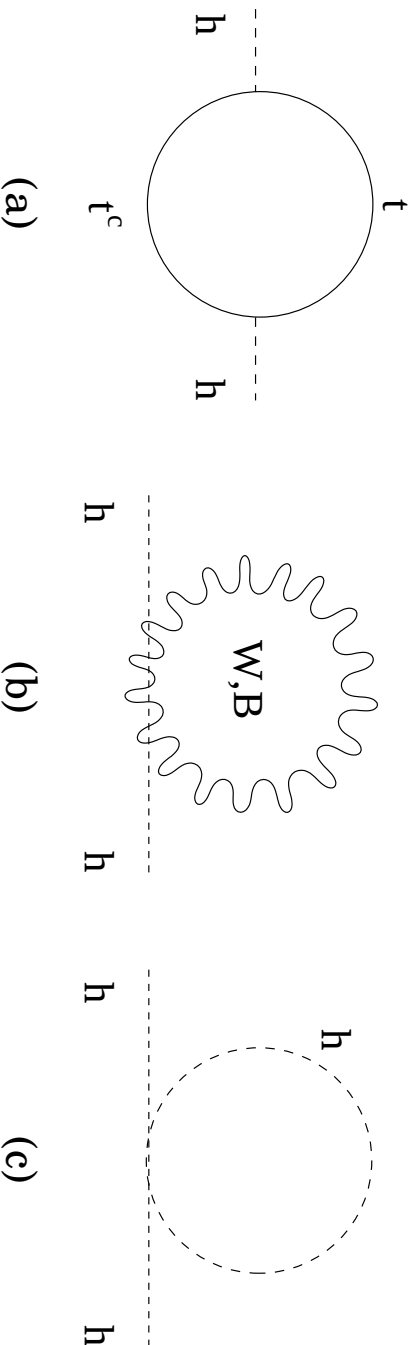


$$m_H^2 = m_{H0}^2 - \frac{3}{8\pi^2} y_t^2 \Lambda^2 + \frac{1}{16\pi^2} g^2 \Lambda^2 + \frac{1}{16\pi^2} \lambda^2 \Lambda^2$$

$$(200 \text{ GeV})^2 = m_{H0}^2 + [- (2000 \text{ GeV})^2 + (700 \text{ GeV})^2 + (500 \text{ GeV})^2] \left(\frac{\Lambda}{10 \text{ TeV}} \right)^2$$

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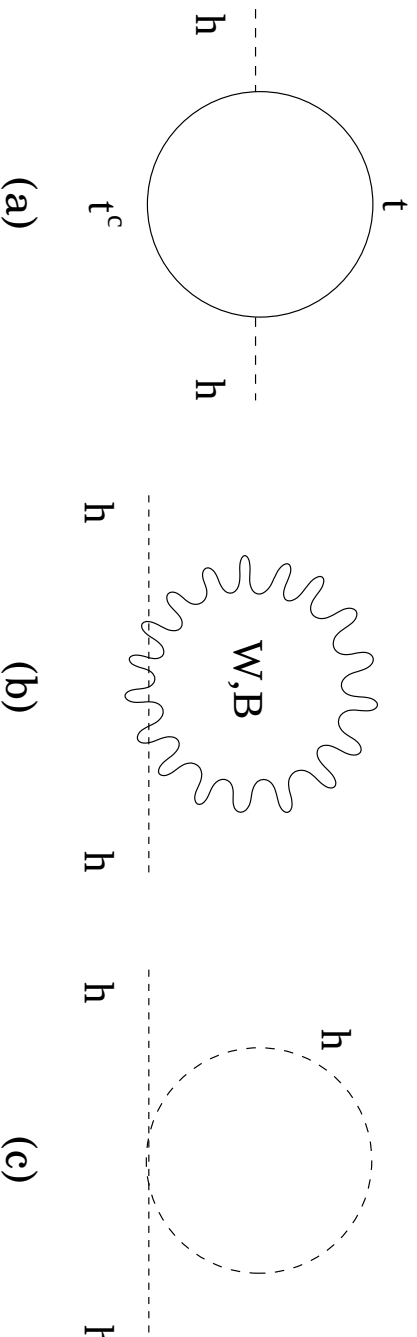
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If requiring less than 90% cancellation, $\Lambda \lesssim 3 \text{ TeV}$ ($\sim 4\pi v$).

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Naturalness requirement: New physics appears at or below 3 TeV.

Yet Another Large Hierarchy: all way down to m_ν

- The simplest (Majorana) neutrino mass term
$$\frac{y_\nu}{\Lambda} H L H L \sim y_\nu \frac{v^2}{\Lambda} \overline{(\nu_L)^c} \nu_L.$$

Taking $m_\nu \lesssim 1 \text{ eV}$,

$$\Rightarrow \Lambda \sim y_\nu \frac{2v^2}{m_\nu} \gtrsim y_\nu (10^{14} \text{ GeV}).$$

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The smaller the fermion masses are, the larger the new physics scale is!

Physics way beyond the SM!

The “Little Hierarchy”: $4\pi v - \Lambda_{new}$

On the one hand, the “naturalness” argument prefers

$$\Lambda_{new} \lesssim 4\pi v, \text{ just like in QCD: } \Lambda_{QCD} \lesssim 4\pi f_\pi.$$

On the other hand,

- EW precision data indicate “decoupling” behavior *
 $\Lambda_{new} \gtrsim 2 - 10 \text{ TeV}.$

(based on generic dim-6 operators.)

- FCNC ($K^0 - \bar{K}^0$ mixing etc.) constraints set
 $\Lambda_{flavor} \gtrsim 70 - 100 \text{ TeV}.$

(based on generic strong dynamics,[†] or generic MSSM[‡])

* Barbieri, Strumia, hep-ph/9905281.

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$\Rightarrow$ imply special structure or symmetry.

Physics just beyond the SM!

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Theoretical issues to address:

- Vastly different mass scales:
EW gauge symmetry breaking;
charged fermion masses;
neutrino masses.
- Nontrivial fermion structure:
three fermion generations;
quark small mixing; neutrino (nearly) maximal mixing;
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- Unified description:
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⇒ All indicate the need for physics beyond the SM.

Our “theory bank”

Let's focus on the EW/SB sector.

Our “theory bank”

Let's focus on the EWSB sector.

(A). Dynamical approach for mass generation:

- Technicolor: a lesson from QCD

$SU(N_{TC})$ gauge theory, TC fermions $Q = U, D, \dots$

EWSB by TC-fermion condensation at Λ_{TC} :

$$v \sim \langle \overline{Q_L} Q_R \rangle^{1/3} \sim 246 \text{ GeV}.$$

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 - ✓ predicts new strong dynamics at the TeV scale: $\pi_T, \eta_T, \rho_T, \omega_T \dots$
- ✗ leads to too large radiative corrections:
 $S \approx 0.25 N_{TC}$, while $S_{exp} \sim -0.07 \pm 0.11.$
- ✗ no fermion masses.

- Extended Technicolor:* for fermion mass generation

G_{ETC} gauge theory, ETC fermions: $U, D, \dots, u, d, \dots$

After integrating out ETC gauge bosons at the scale Λ_{ETC} , with TC-fermion condensate, SM fermion mass generated:

$$m_f \sim \langle \overline{Q_L} Q_R \rangle / \Lambda_{ETC}^2 \sim \Lambda_{TC}^3 / \Lambda_{ETC}^2.$$

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For a review, Hill and Simmons

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✗ a devastating problem:

On the one hand: small FCNC: $\frac{1}{\Lambda_{ETC}} < \frac{1}{10^3 \text{ TeV}}$.

on the other hand, heavy quark $m_c \sim 1 \text{ GeV} \Rightarrow \Lambda_{ETC} < 30 \times \frac{\Lambda_{TC}}{1 \text{ TeV}}$

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$\Rightarrow$ Non-QCD like: Walking TC

TC gauge coupling running very slowly.

$\langle \overline{Q_L} Q_R \rangle$ almost constant over $\Lambda_{TC} - \Lambda_{ETC}$.

$\langle \overline{Q_L} Q_R \rangle_{ETC}$ enhanced by 100–1000.

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- “Topcolor/Top-seesaw”: Top quark special ?
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Introducing an additional fermion pair χ_L, χ_R :

(1) topcolor^{*} generates the condensation $H \sim (\bar{\chi}_R t_L, \bar{\chi}_R b_L)$

$\Rightarrow$ EWSB and a heavy Higgs $m_H \sim 1 \text{ TeV}$.

(2) topseesaw[§] leads to a SM t , and a heavy state χ , with $M_\chi \approx 4 \text{ TeV}$.

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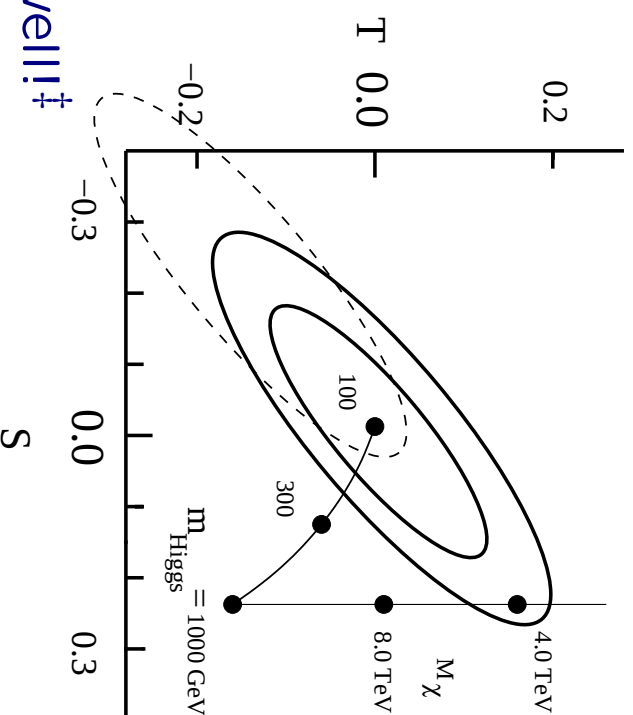
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fit EW precision data well![‡]

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‡ H.-J. He, C. Hill, T. Tait.

- A less ambitious approach: Little Higgs Models
Accept the existence of a light Higgs;
keep the Higgs boson “naturally” light (at 1-loop level).
- † Higgs is a pseudo-Goldstone boson from global symmetry breaking (at scale $4\pi f$)[†]
- † Higgs acquires a mass radiatively at the EW scale v , by collective explicit breaking
- † Consequently, quadratic divergences absent at one-loop level*

$$W, Z, B \leftrightarrow W_H, Z_H, B_H; \quad t \leftrightarrow T; \quad H \leftrightarrow \Phi.$$

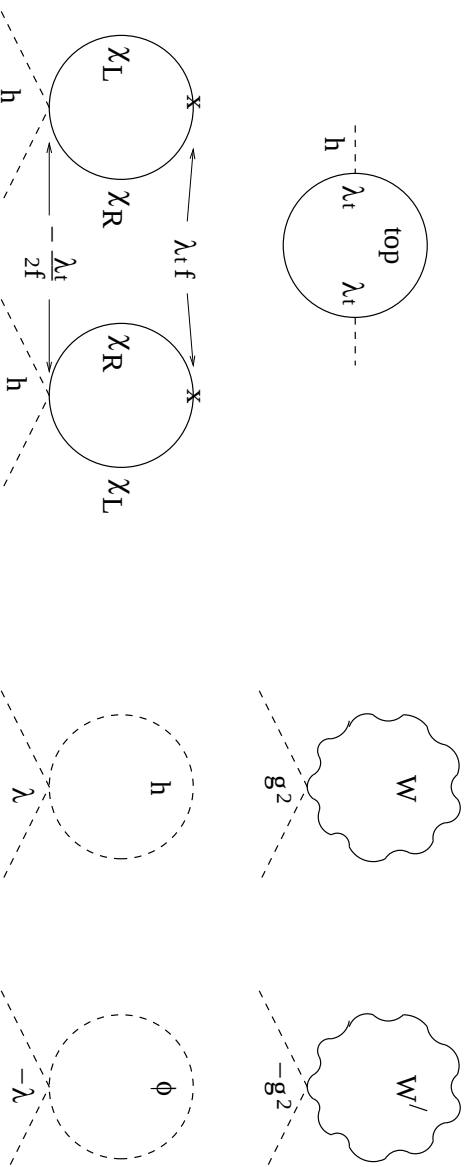
(cancellation among same spin states!)

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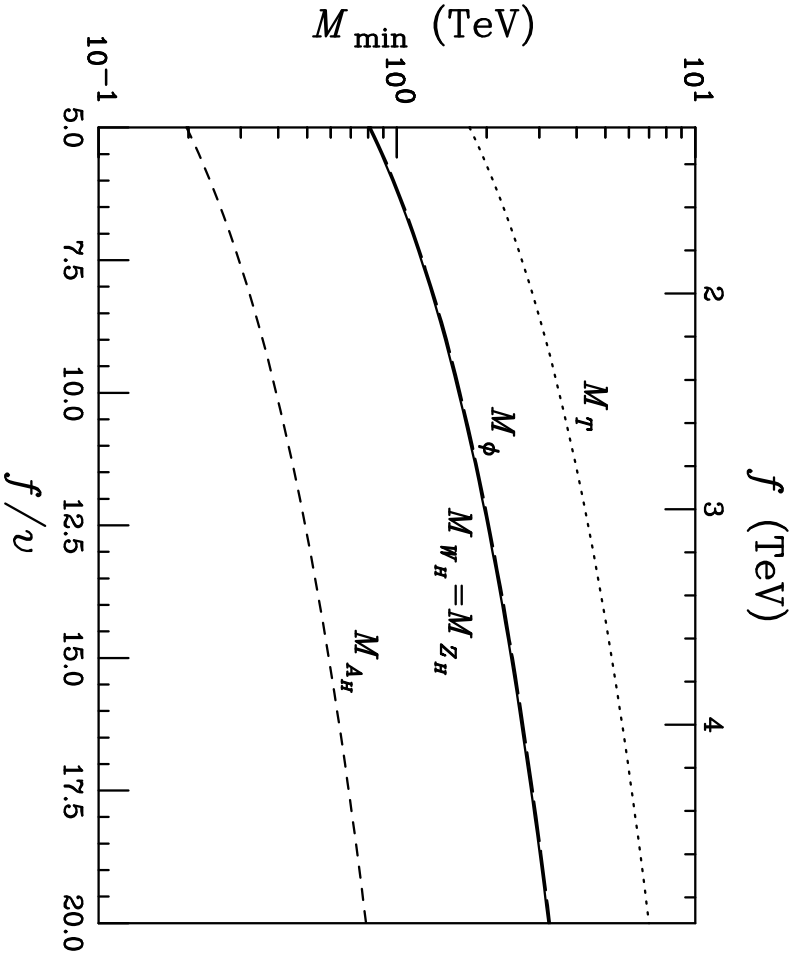
An alternative way to keep H light (naturally)

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New heavy states in the littlest Higgs:

Heavy particles	
T	$\frac{\text{Mass}}{\sqrt{\lambda_1^2 + \lambda_2^2}} f$
Z_H	$m_W^2 \frac{f^2}{s^2 c^2 v^2}$
W_H	$m_W^2 \frac{f^2}{s^2 c^2 v^2}$
$\phi^0, \pm, \pm\pm$	$\frac{2m_H^2 f^2}{v^2} \frac{1}{1-(4v'f/v^2)^2}$
A_H	$m_z^2 s_W^2 \frac{f^2}{5s'^2 c'^2 v^2}$



$$(m_h \approx 115 \text{ GeV})$$

(B). Weak-scale Supersymmetry:

A natural cancellation mechanism:

Symmetry between opposite spin & statistics

$\tilde{t}$ versus t

$\tilde{W}$ versus W

$\tilde{H}$ versus H

H_d versus H_u ,

(B). Weak-scale Supersymmetry:

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H_d versus H_u ,

$$\Delta m_H^2 \sim (M_{SUSY}^2 - M_{SM}^2) \frac{\lambda_f^2}{16\pi^2} \ln \left(\frac{\Lambda}{M_{SUSY}} \right).$$

Weak scale SUSY stabilizes the hierarchy $M_W - M_{pl}$

only if the “soft-SUSY breaking”: $M_{SUSY} \sim \mathcal{O}(M_{SM})$.

✓ predict TeV scale new physics:

light Higgs bosons H^0 , A^0 , $H^\pm$; SUSY partners $\tilde{W}^\pm \dots$, $\tilde{g}$, $\tilde{q}$, $\tilde{l}^\pm \dots$

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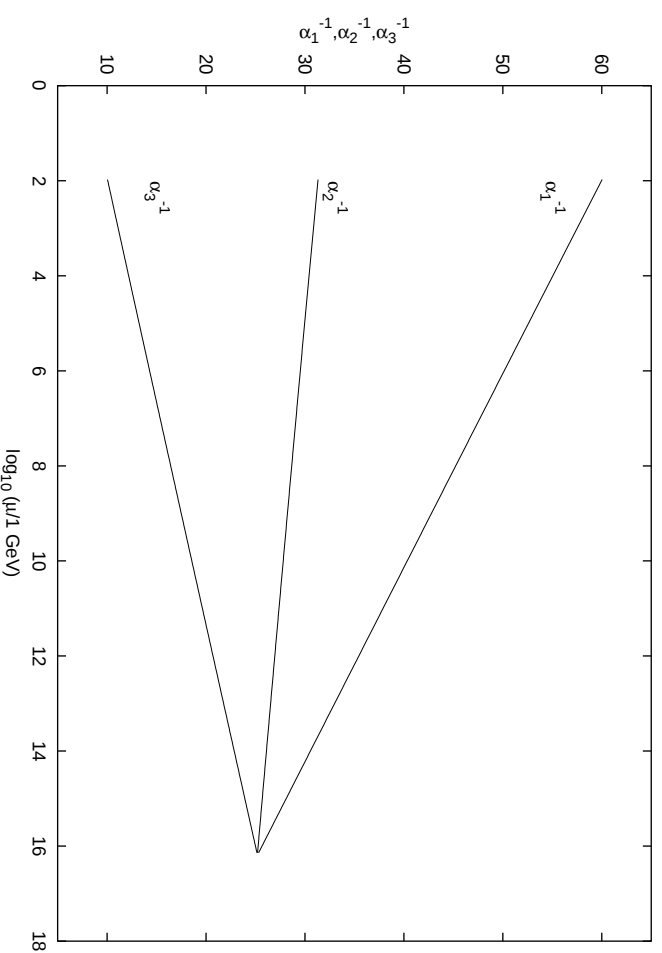
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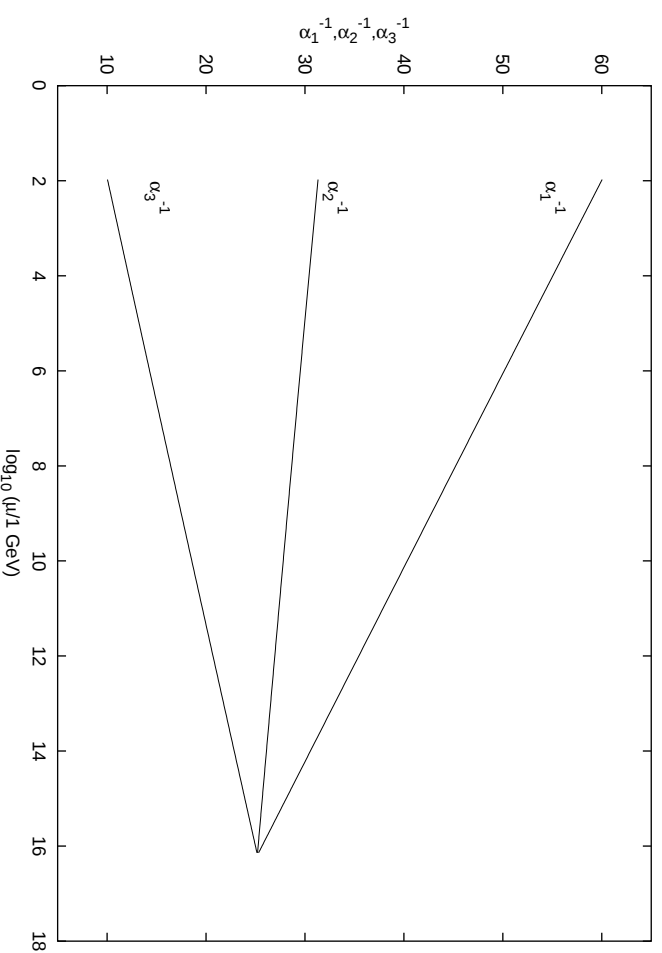
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✓ The “LSP” is a good dark matter candidate $\tilde{\chi}^0 \sim \tilde{B}$.

What about M_{SUSY} ?

- ✗ Supersymmetry breaking mechanism is unknown.
Merely (124?) free parameters;
most part of the parameter-space ruled out.

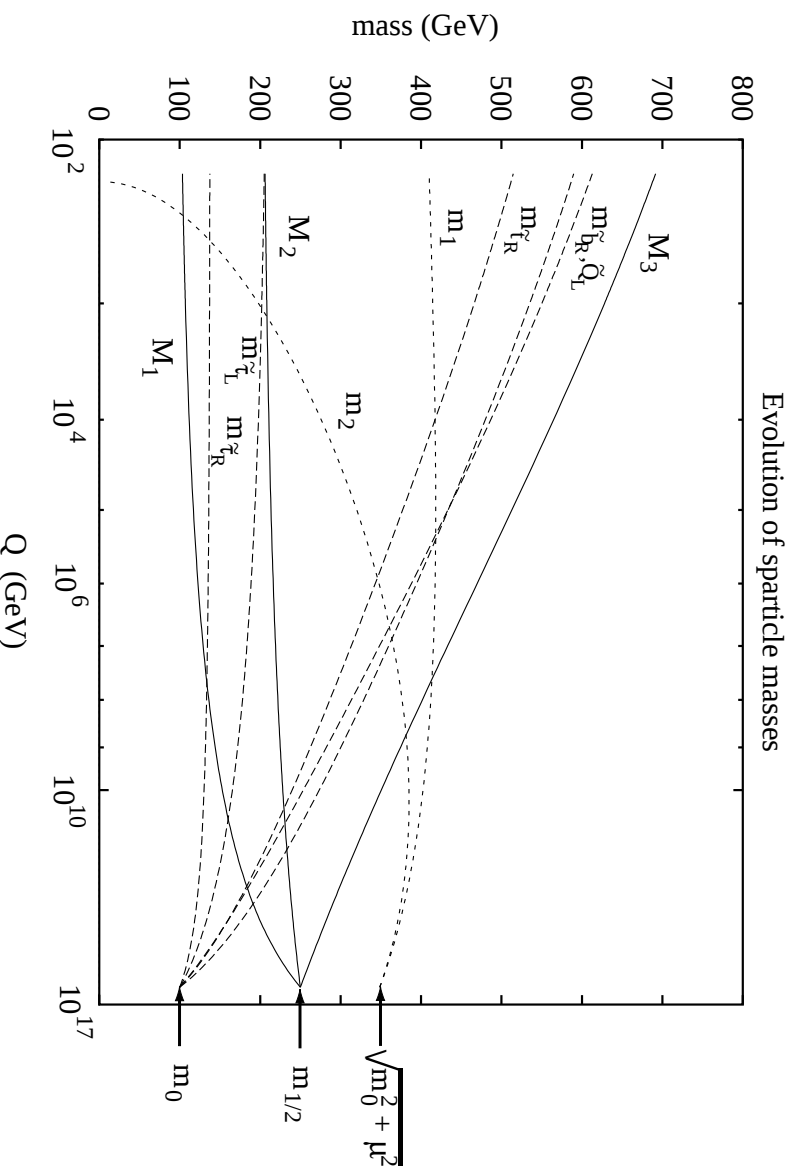
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Assumption on the parameters: $SUSY$ breaking in a hidden sector

(*) mSUGRA scenario: m_0 , $m_{1/2}$, A , $\tan\beta$, and $sign(\mu)$

(*) Gauge mediation scenario: M , F , $\tan\beta$, nm .

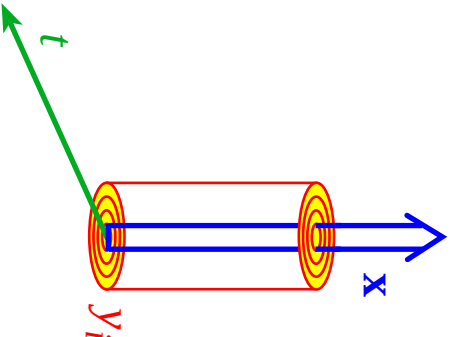


A new approach to the hierarchy problem

- Large Extra-dimension Scenario; ADD^{*}

In a world with $D = 4 + n$ dimensions, the 4-dim Planck scale is related to the D-dim one M_D as

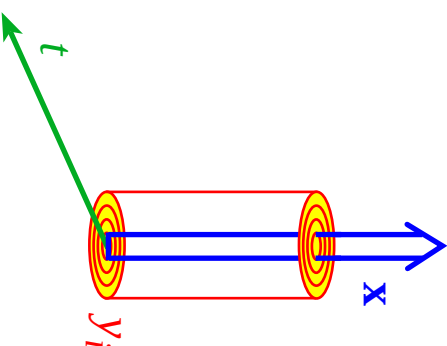
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(C). Extra-dimensions: A new approach to the hierarchy problem

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Thus the fundamental scale:

$$M_D \sim (M_{pl}^2/V_n)^{n+2} \longrightarrow \mathcal{O}(1 \text{ TeV}).$$

or the radius:

$$R \sim \frac{M_{pl}^{2/n}}{M_D^{2/n+1}} \approx \begin{cases} \mathcal{O}(0.1 \text{ mm}) & \text{for } n = 2 \\ \mathcal{O}(1.0 \text{ fm}) & \text{for } n = 7 \end{cases}$$

- “Warped” Extra-dimension Scenario; the Randall-Sundrum model

In a 5-dim space, Randall and Sundrum found a static solution of the form:*

$$ds^2 \sim e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2,$$

where k is the curvature scale in the 5th-dim.

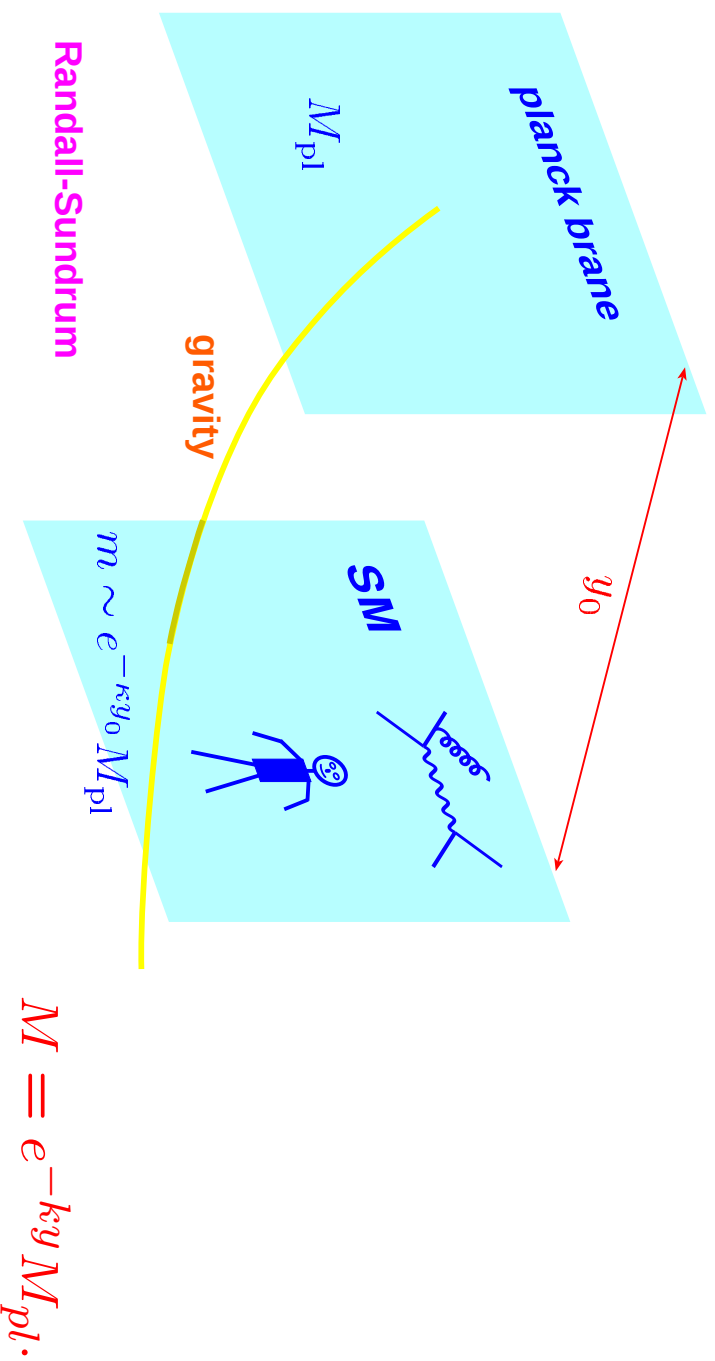
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The extra dimension y is “warped”.



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Symmetry breaking by boundary conditions/terms

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5d SUSY GUTs model, with SUSY/GUT symmetry breaking by orbifolding on the boundary.

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5d non-SUSY model, with gauge symmetry breaking by orbifolding/boundary condition.

Bulk KK states serve as pseudo-Glodonstone bosons, no Higgs left.

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Particularly interesting: AdS/CF_T correspondence

5d AdS theory $\longleftrightarrow$ 4d strongly interacting walking TC!

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- Observable signatures for extra-dim models:
 - ▷ At “low” energies
 - † “very low”: $E \ll 1/R, M_D$:
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mainly via light KK gravitons of mass

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or whatever propagate there $\Rightarrow$ an effective theory (SM+KK).

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▷ Intermediate energy regime $E \sim M_D$: stringy states significant:†
 s -channel poles as resonances:†

$$\mathcal{M}(s, t) \sim \frac{t}{s - M_n^2}, \quad M_n = \sqrt{n} M_S.$$

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† G. Shui and H. Tye (1998); K. Benakli (1999).

† Accomando, Antoniadis, Benakli (2000); Cullen, Perelstein, Peskin (2000).

▷ At “trans Planckian” energies $E > M_D, M_S$:
(4 + n)–dim physics directly probed;
gravity dominant: black hole production[‡]

$$\sqrt{s} = M_{BH} > M_D \text{ for } b < r_{bh}.$$

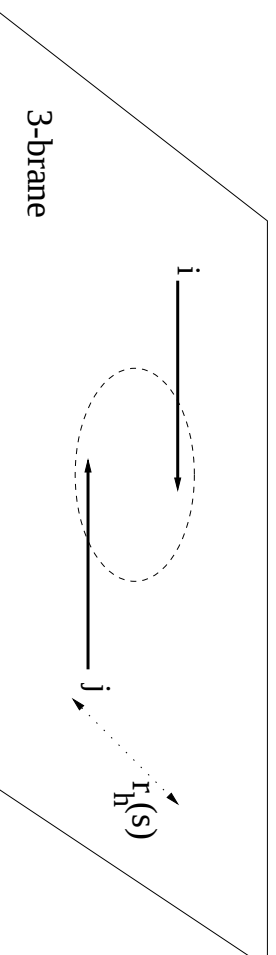
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$$r_{bh} = \frac{1}{\sqrt{\pi} M_D} \left[\frac{M_{BH}}{M_D} \left(\frac{8\Gamma\left(\frac{n+3}{2}\right)}{n+2} \right) \right]^{\frac{1}{n+1}} \rightarrow M_{BH}/M_{pl}^2 \text{ in 4d}$$

$$\sigma = \pi r_{bh}^2.$$



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Yet more to come:

Tevatron: EW, top sector, Higgs (?), new particle searches...

LHC: Higgs studies, comprehensive new particle searches...

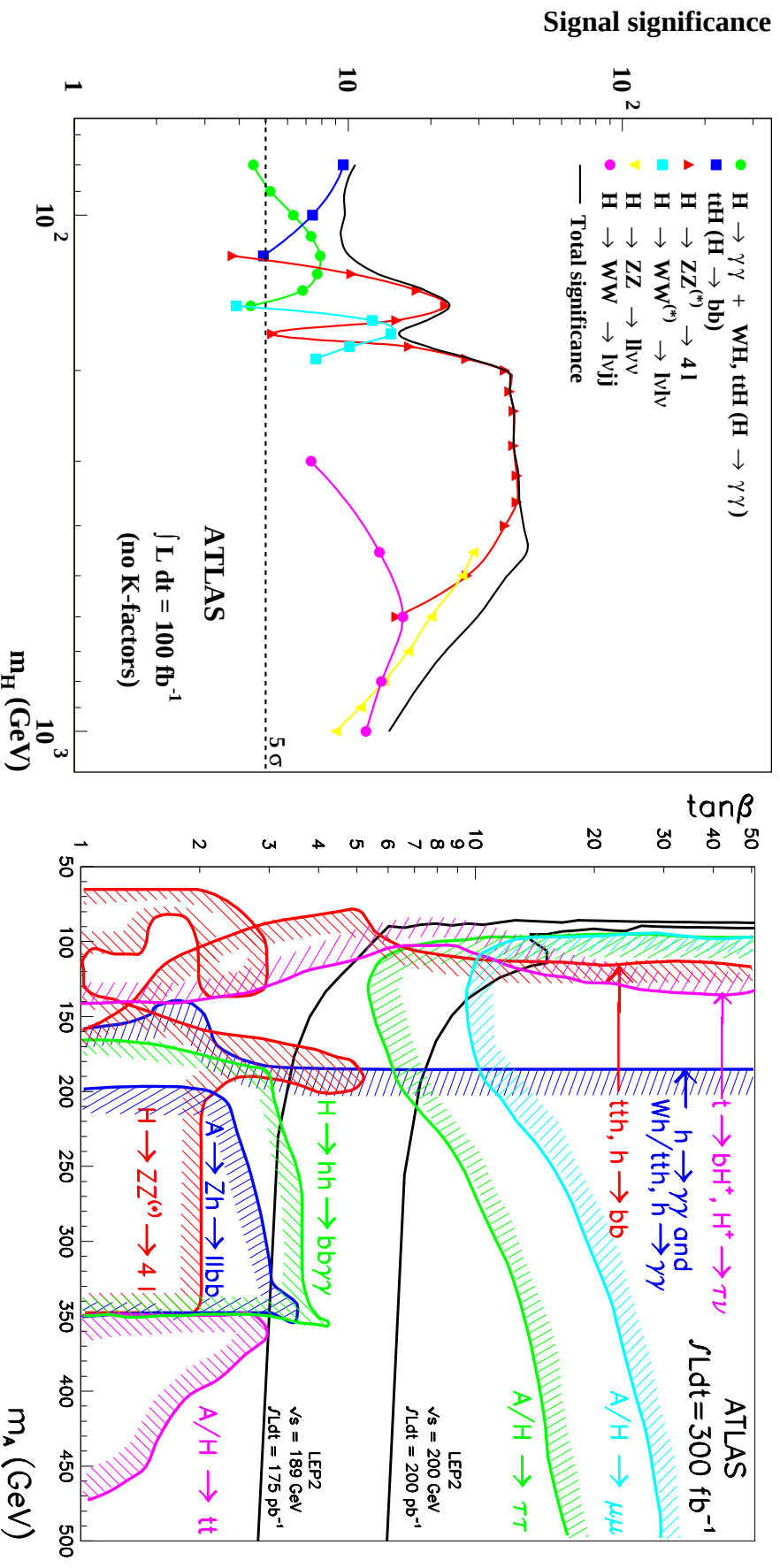
LC: more on top sector, precision Higgs and new light particles...

Other complementary experiments: non-accelerators ...

New Physics at Future Hadron Colliders

For any scenario beyond SM, LHC WILL contribute:

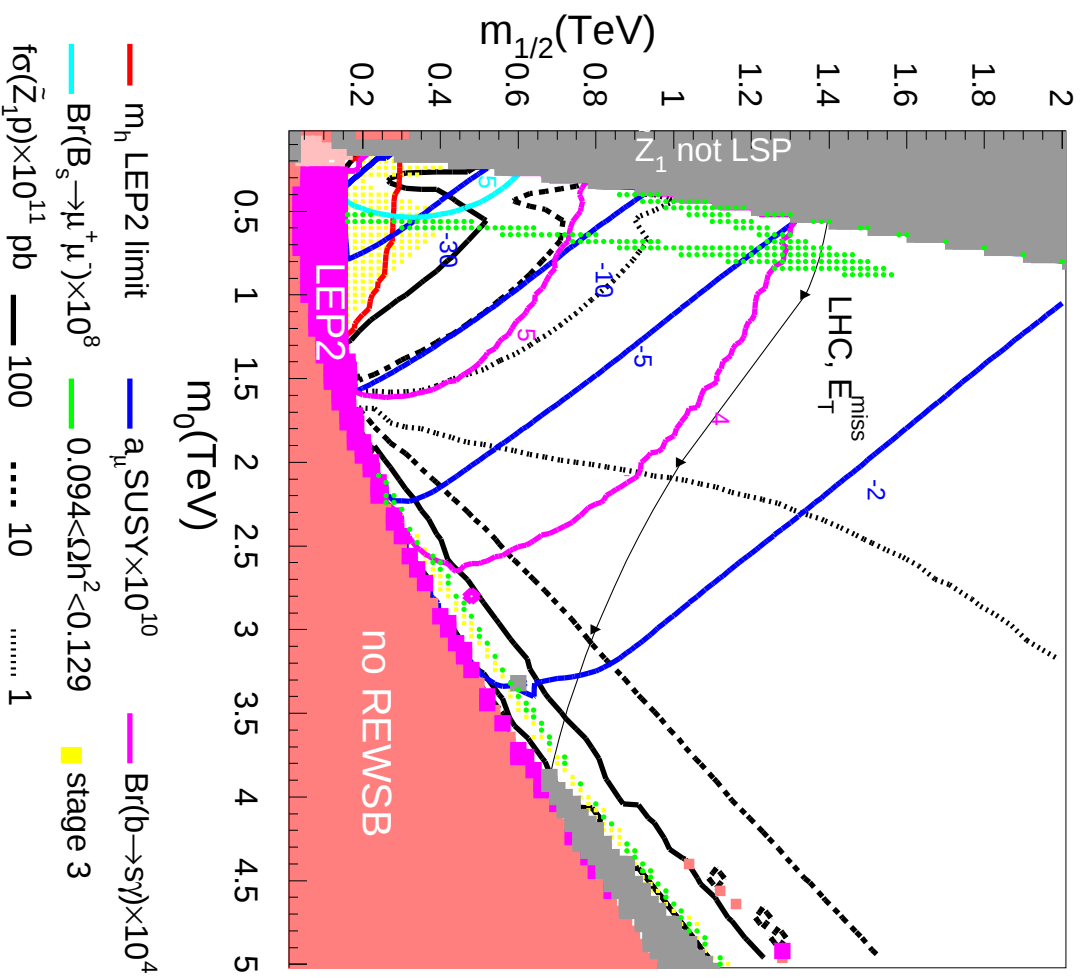
- Higgs fully covered at the LHC:



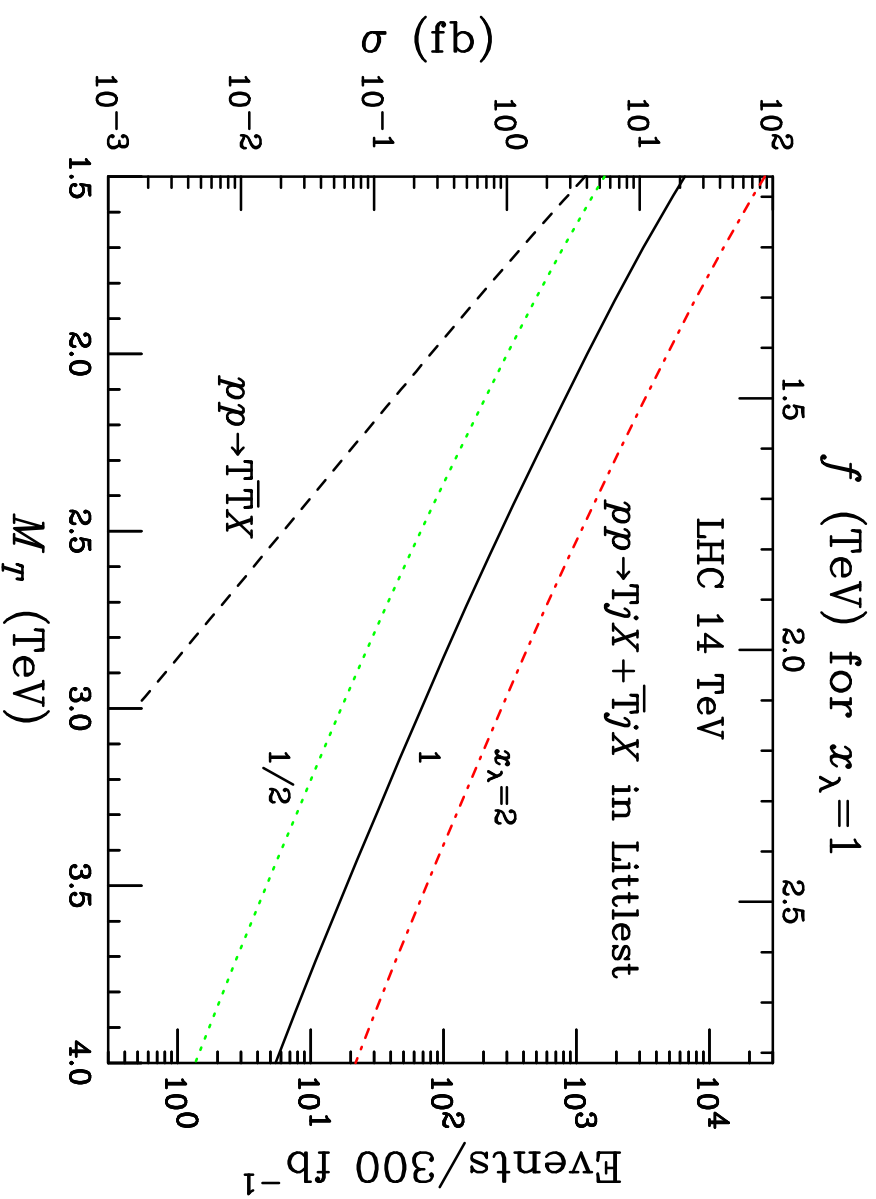
- LHC will have great chance for SUSY discovery: *

$m_0 > 4000 \text{ GeV}$, $m_{1/2} > 1400 \text{ GeV}$, $\tan\beta \gtrsim 45$.

mSUGRA: $\tan\beta=45$, $A_0=0$, $\mu<0$



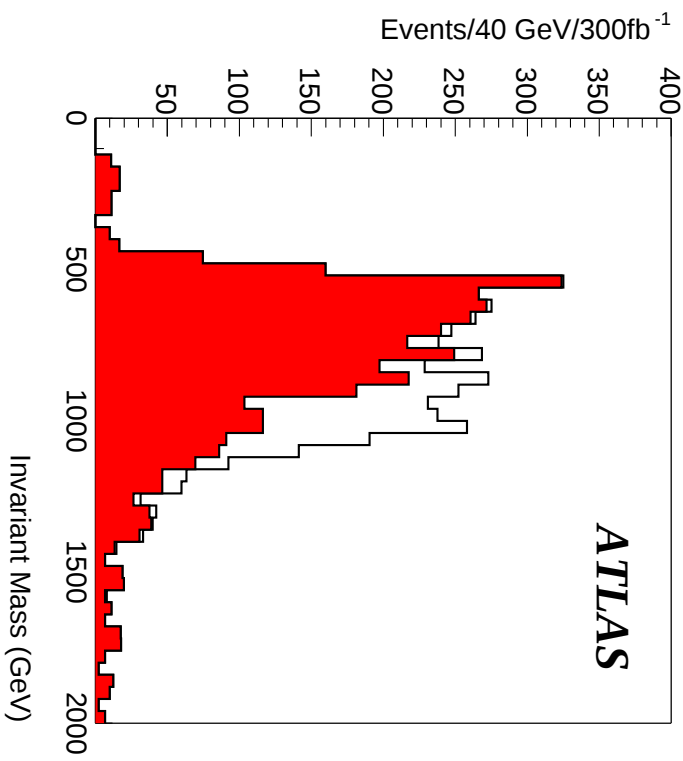
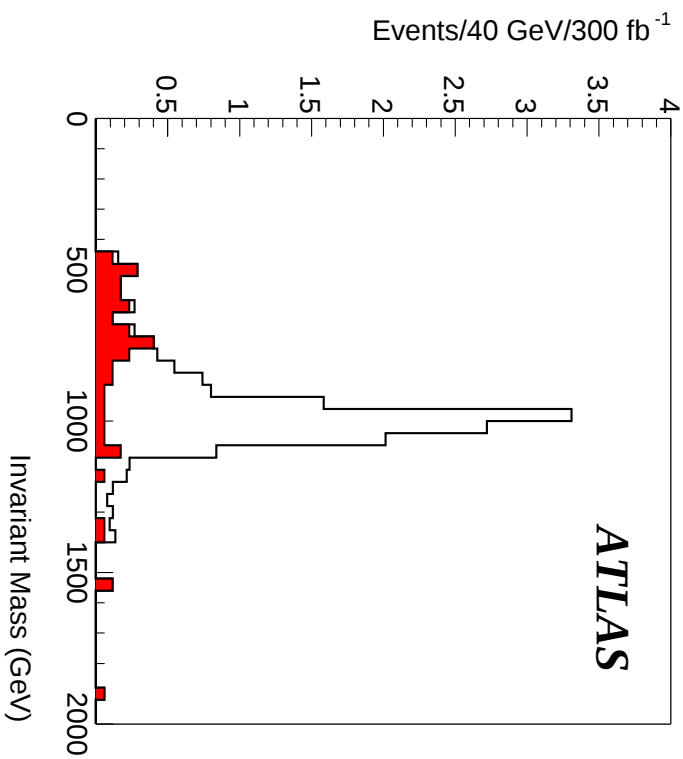
- LH: The heavy T signal at LHC



$gg \rightarrow T \bar{T}$ phase-space suppression;

$qb \rightarrow q' T$ via t -channel $W_L b \rightarrow T$.

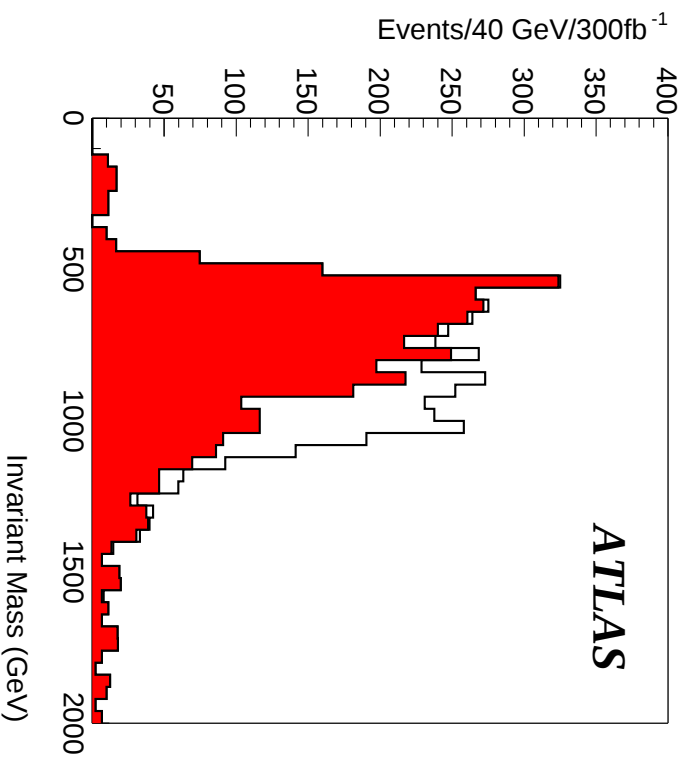
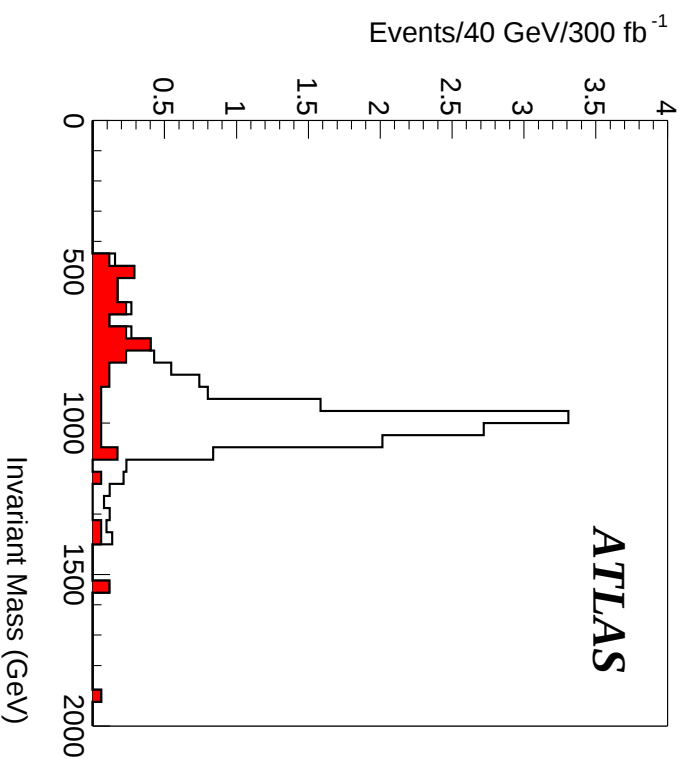
ATLAS simulations for $T \rightarrow tZ$, bW .*



Reach $M_T \sim 1$ (2) TeV for $x_\lambda = 1$ (2).

*G. Azuelos et al.: hep-ph/0402037.

ATLAS simulations for $T \rightarrow tZ$, bW .*



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Cross-sections measure coupling x_λ .

Mass peak M_T determines $f : v/f = m_t/M_T(x_\lambda + x_\lambda^{-1})$

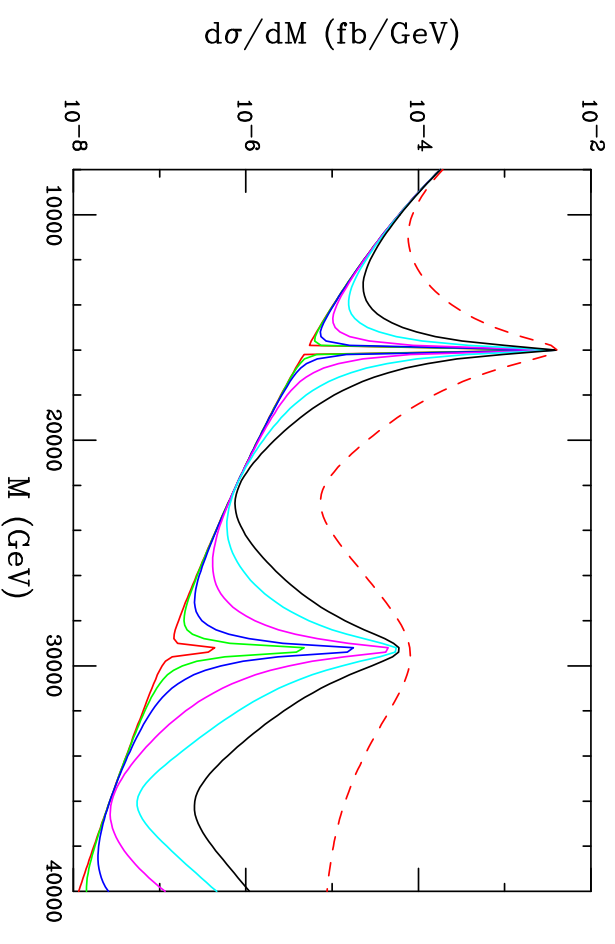
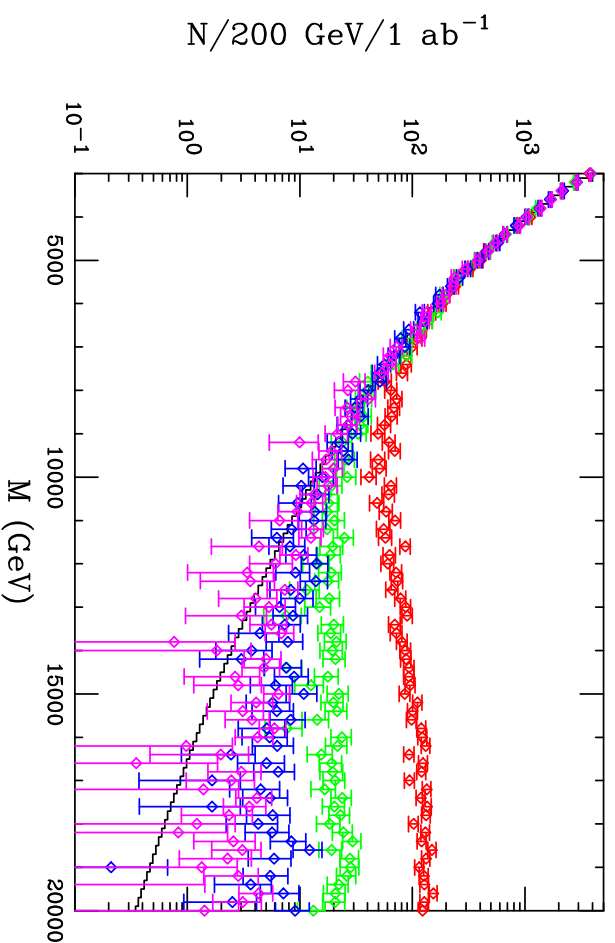
$\Rightarrow$ check consistency with f from M_{Z_H} .*

*G. Azuelos et al.: [hep-ph/0402037](https://arxiv.org/abs/hep-ph/0402037).

*Perelstein, Peskin, Pierce: [hep-ph/0310039](https://arxiv.org/abs/hep-ph/0310039).

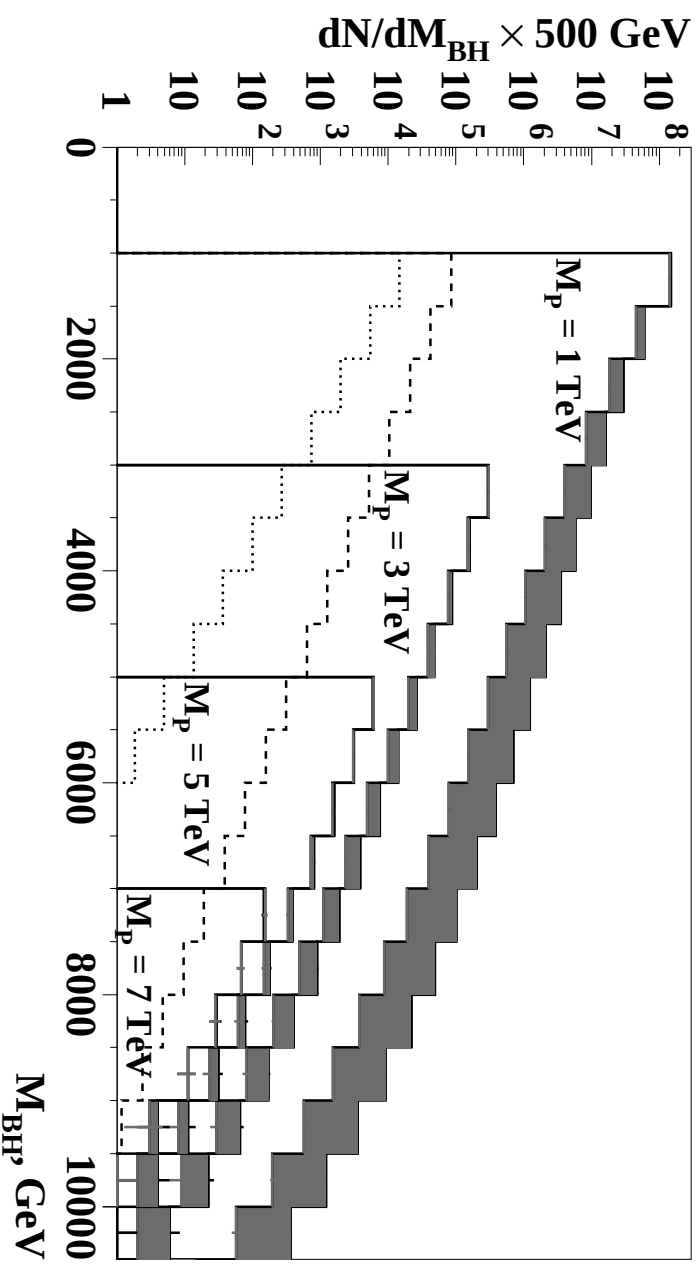
- Deep into extra-dimensions at the LHC:

Large extra-dim ADD & warped extra-dim RS: *



left: ADD with $M_* = 20, 25, 30, 35 \text{ TeV}$;
right: RS with $M_{KK} = 16 \text{ TeV}$.

Black hole to ℓ and γ events at the LHC: *



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- Only experiments can tell.
Go For The LHC!